

Laser Measurement Science

in Gravitational Physics

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&

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Chair and Department Director

Knowledge for Tomorrow



Outline

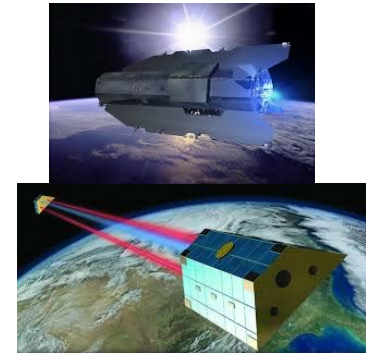
- Gravitational Wave Detectors

- Ground-based observatories
- Space-based observatories: LISA
- LISA Pathfinder



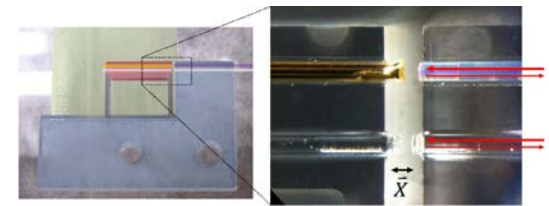
- Earth Observation

- GRACE / GRACE follow-on
- Collaborative Research Center:
 - *geo-Q* Relativistic geodesy and gravimetry



- Novel Optomechanical Technologies

- Concept and overview of results
- Accelerometers
- Gravimeters and Gradiometers
- Micro-optical motion sensors
- Optomechanical Laser: tunable external cavity, THz source
- Force sensors

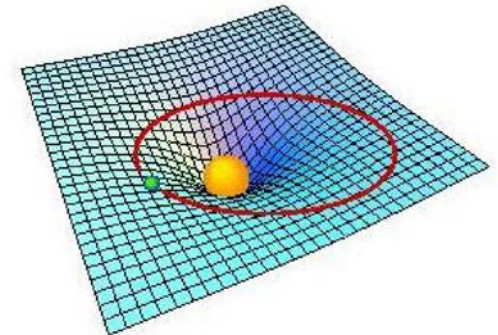
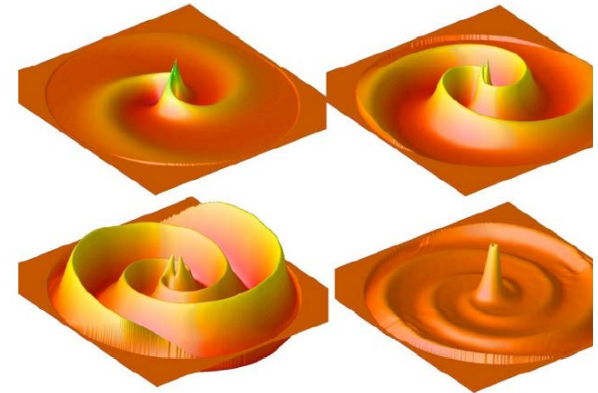
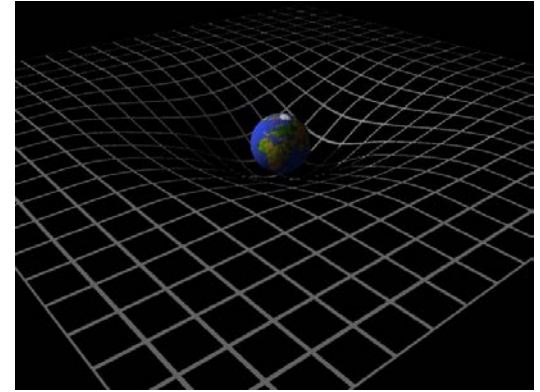


Gravitational Radiation

- 1916. Albert Einstein proposed a new model for Gravitation: General Theory of Relativity.
 - Mass determines spacetime curvature.
 - Curvature determines the movement of the masses.
 - Accelerated masses → Gravitational Waves.

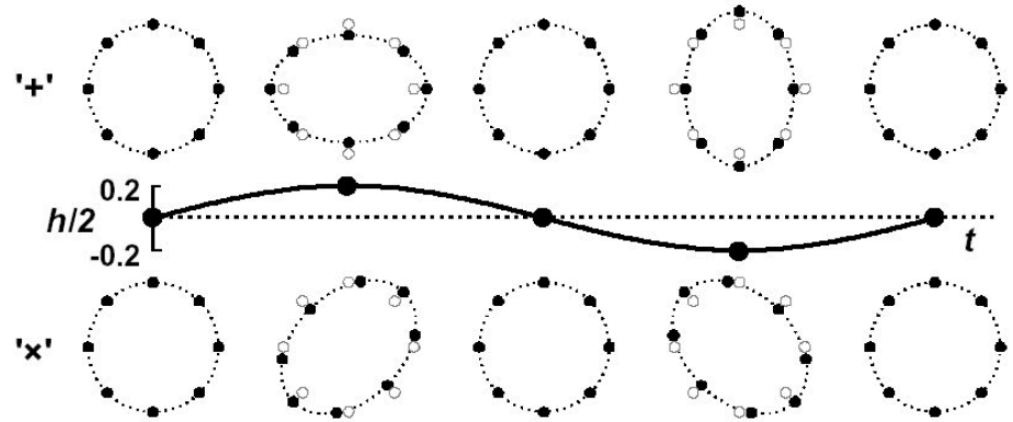
- Current astronomy is based on detection of electromagnetic radiation.
 - Multimessenger Astronomy starting now!

- Gravitational waves: different source of information
 - Early universe
 - Cosmological objects
 - Dark phenomena → no EM radiation

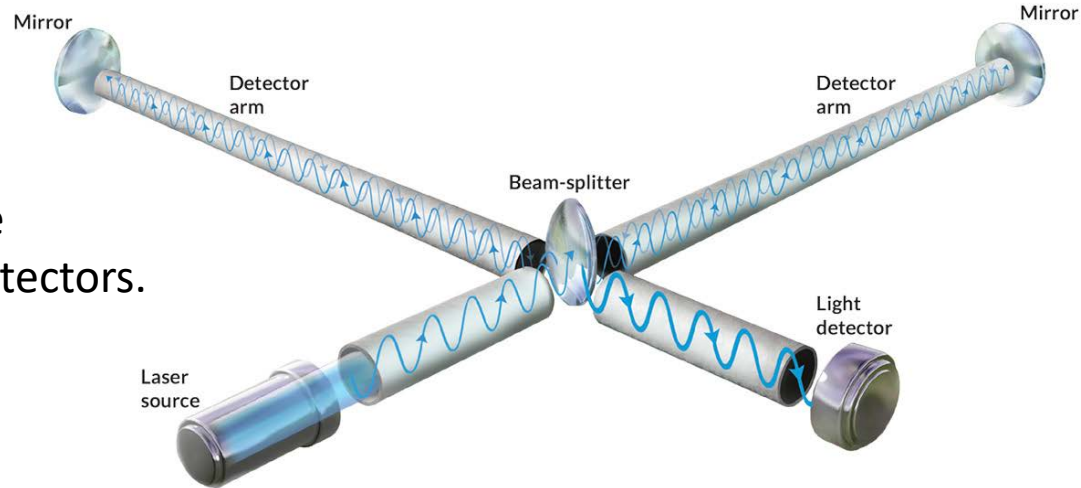


Gravitational Wave Observatories

- Gravitational waves change distances between floating test-masses as they propagate.

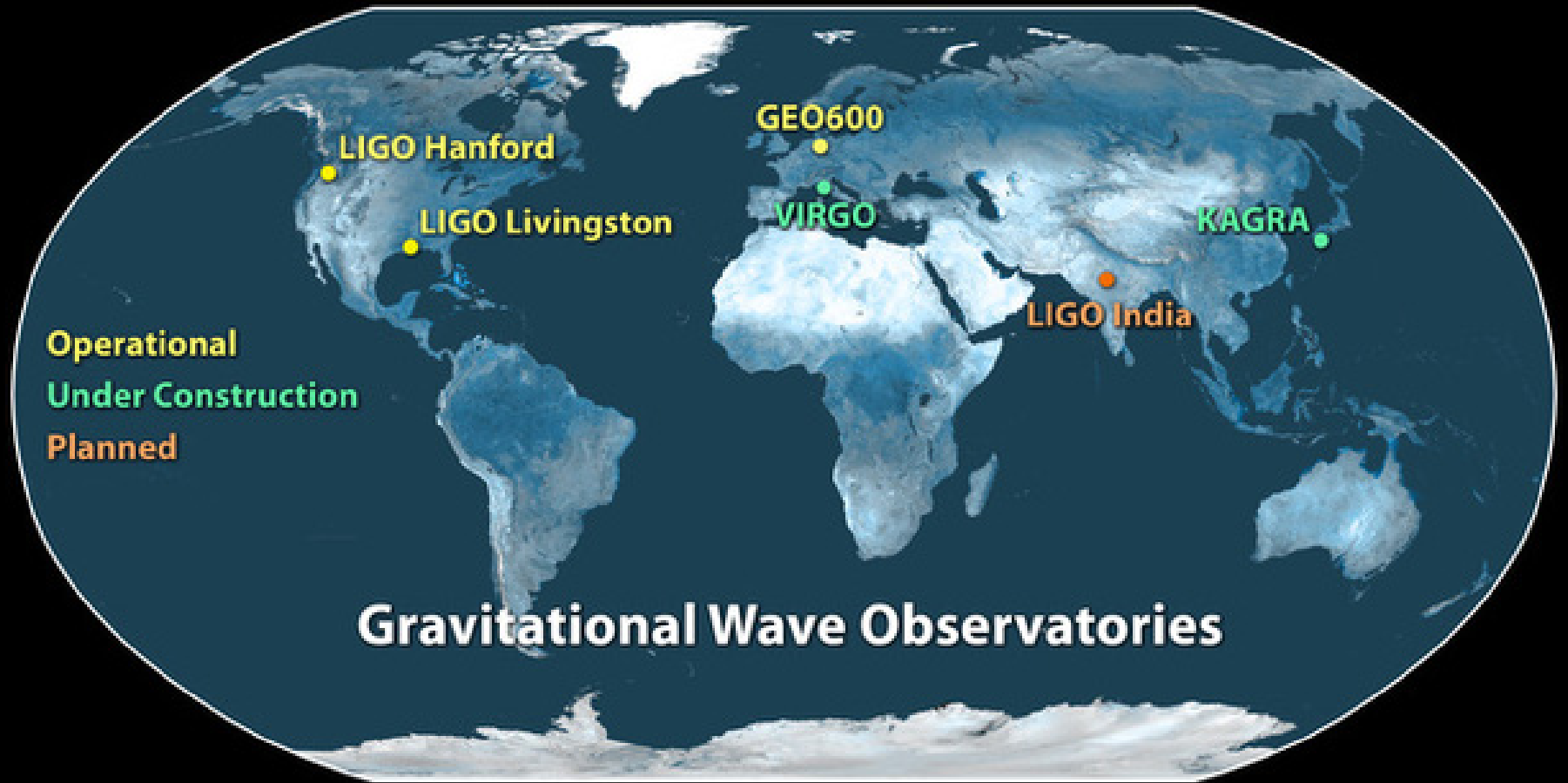


- Interferometers monitor the distance between test masses → ideal GW detectors.



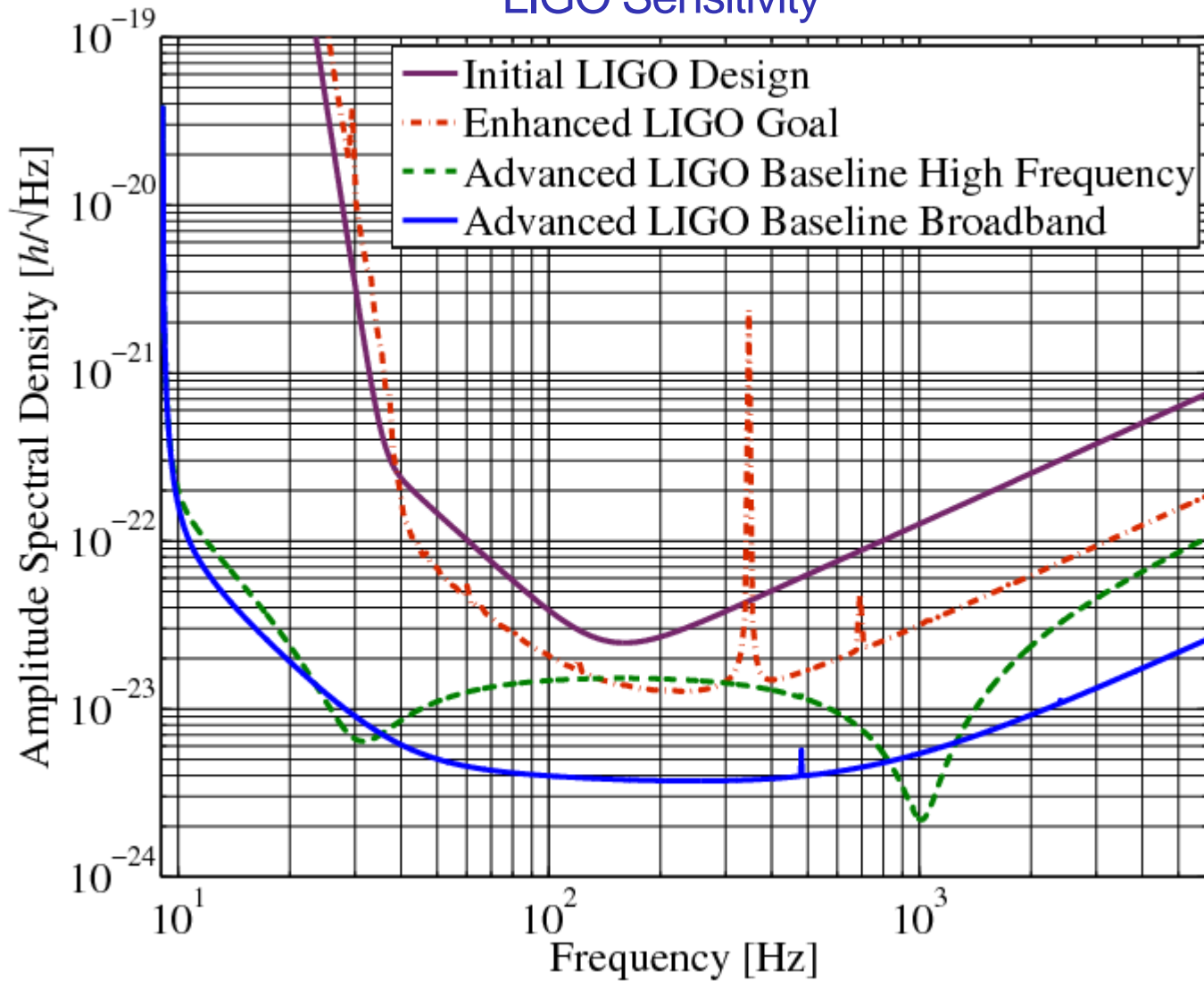
Gravitational Wave Observatories

World Wide Network



Gravitational Wave Observatories

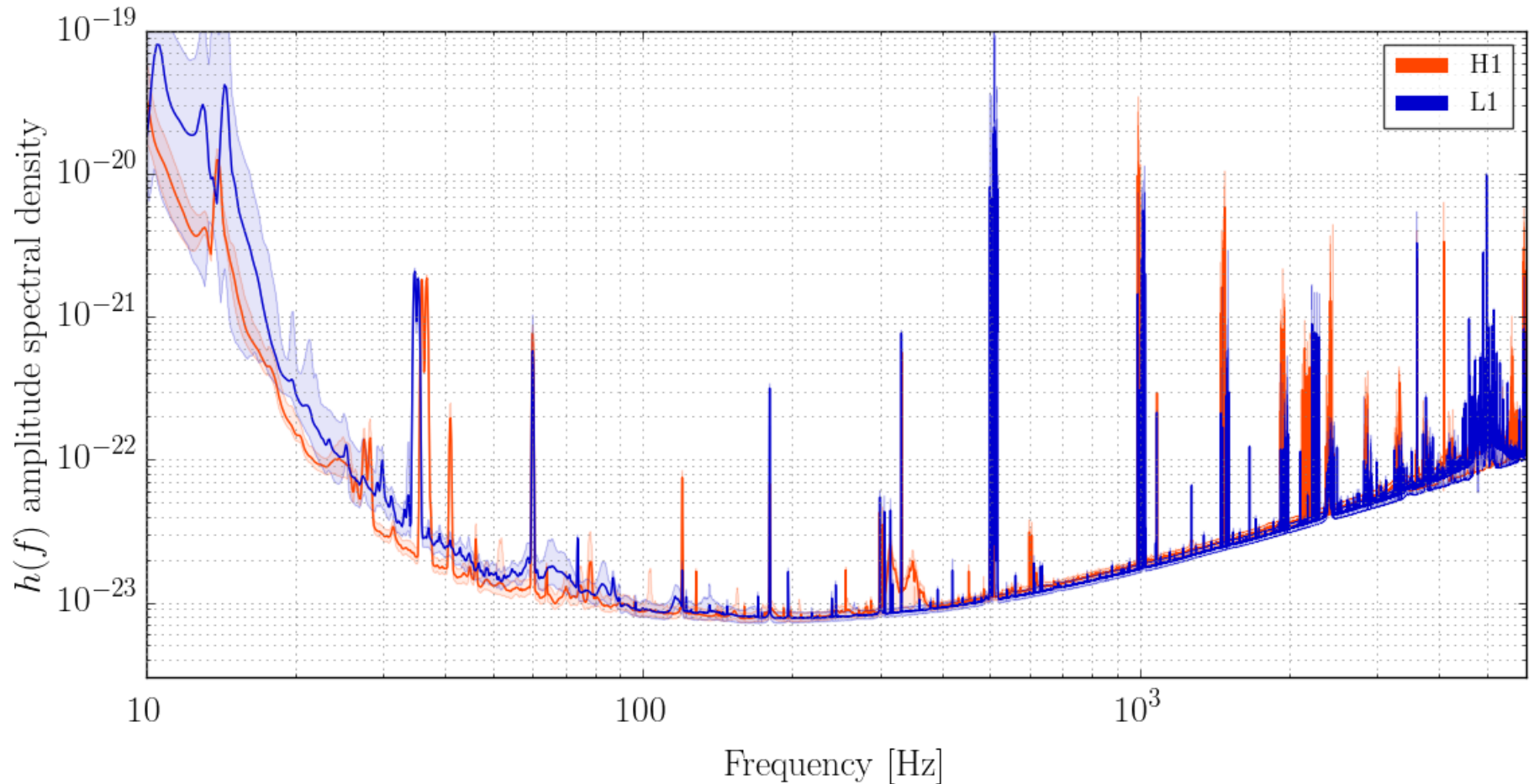
LIGO Sensitivity



Gravitational Wave Observatories

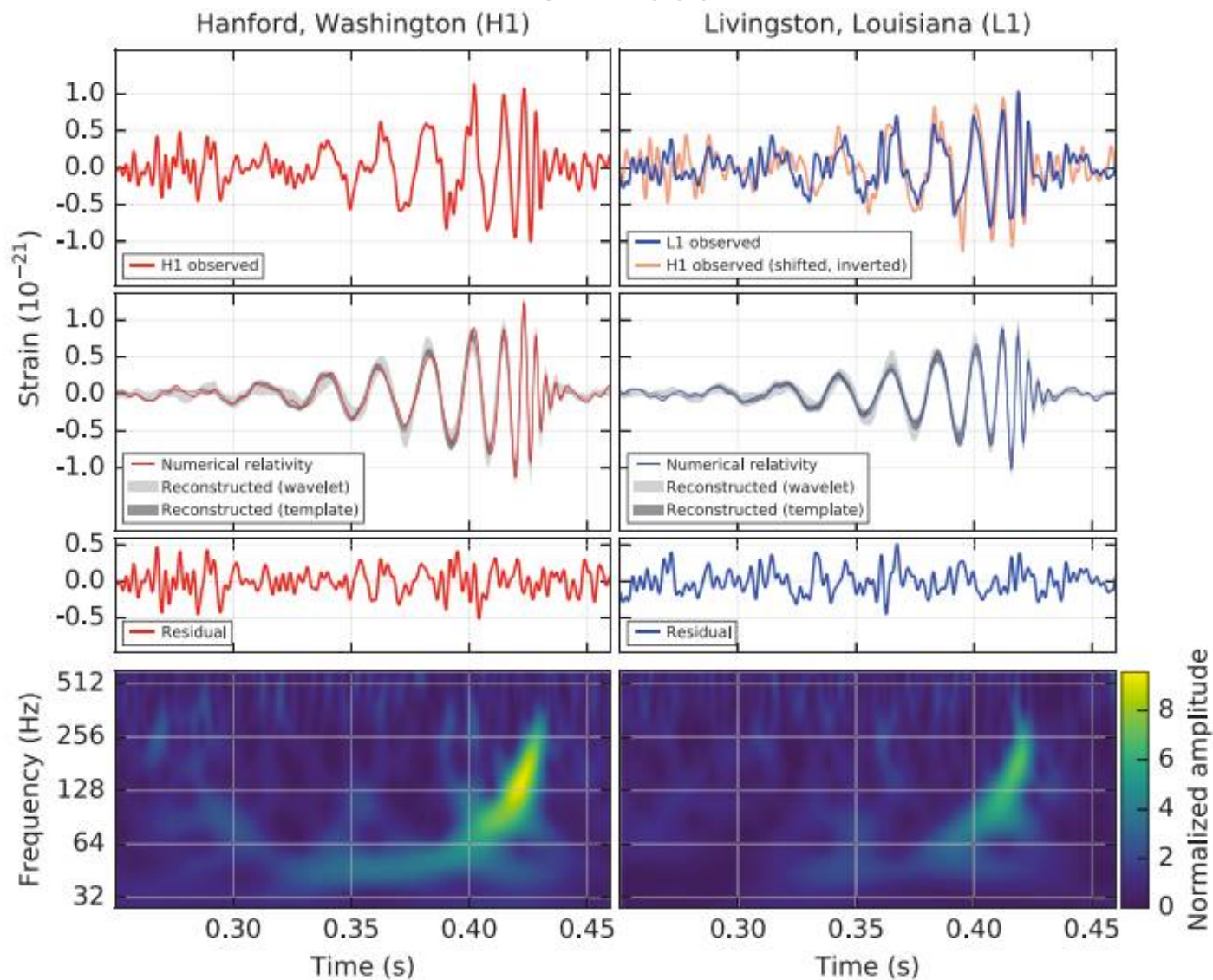
LIGO Sensitivity

$$h(f) = \frac{\delta L(f)}{L} \rightarrow \delta L \approx 10^{-20} \text{ m}/\sqrt{\text{Hz}}$$



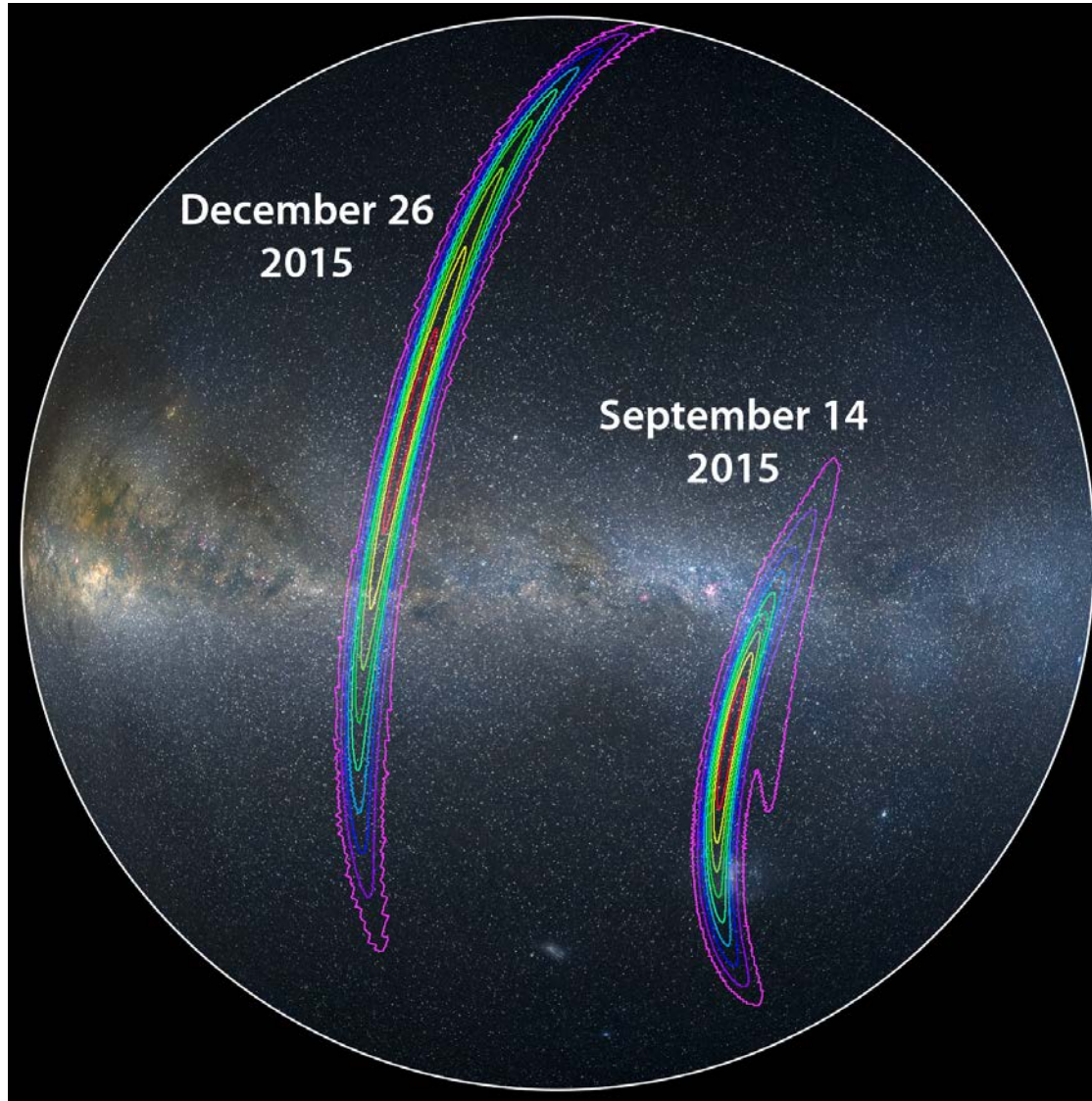
Gravitational Wave Observatories

GW 150914



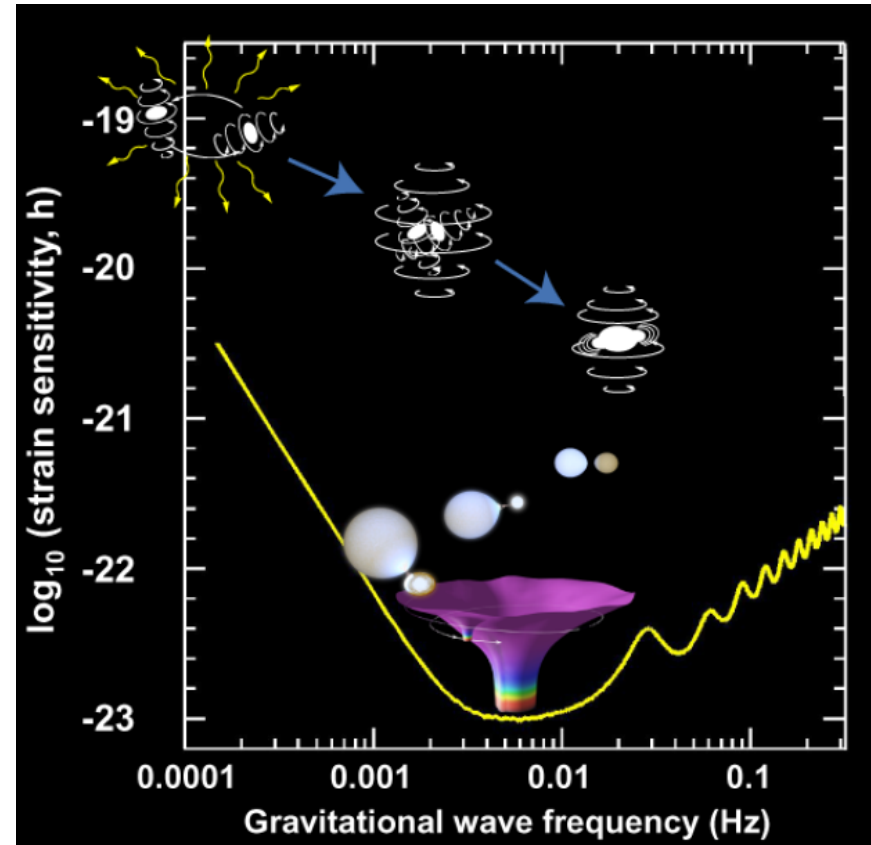
Gravitational Wave Observatories

LIGO observations

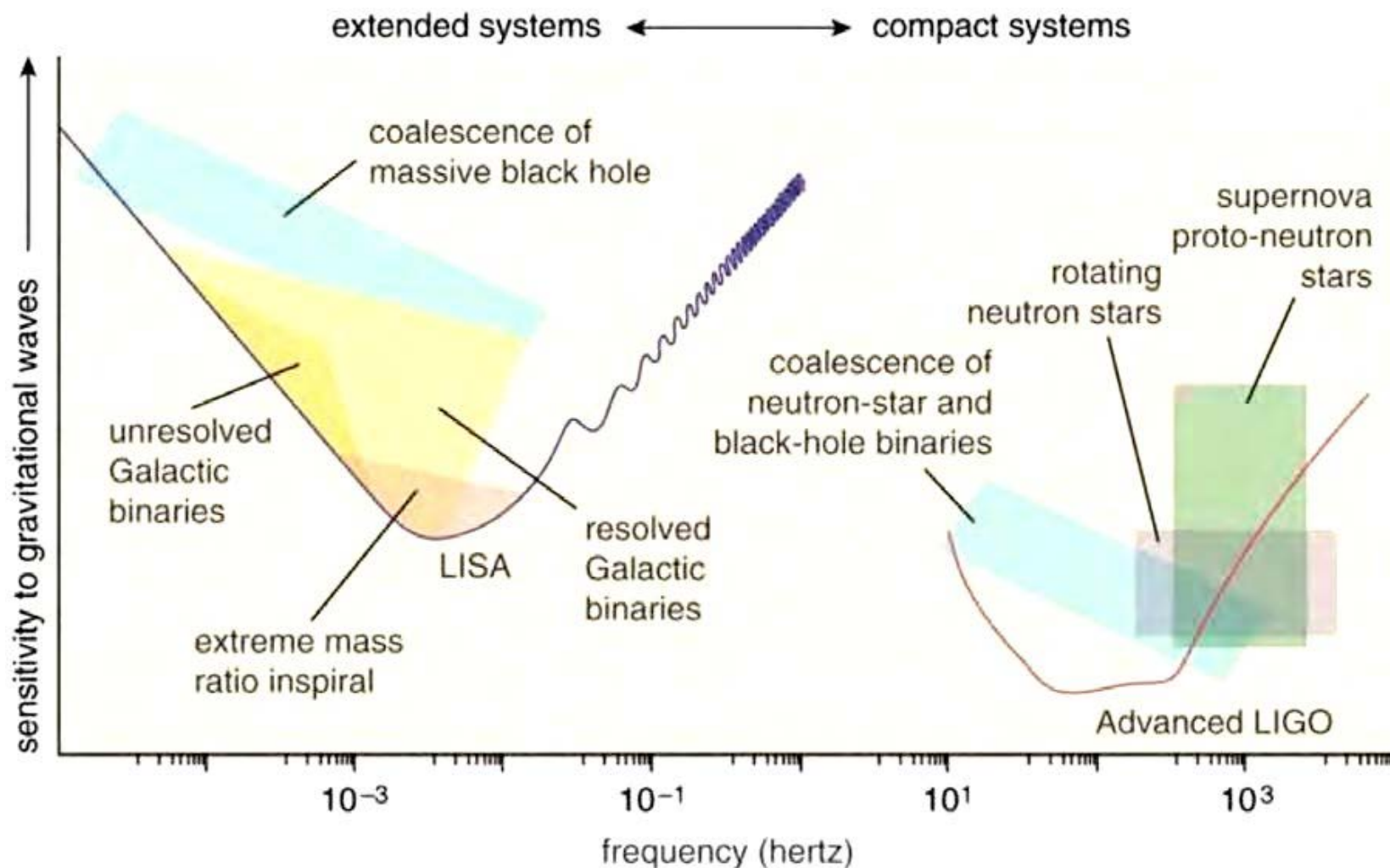


Space-based Observatories - LISA

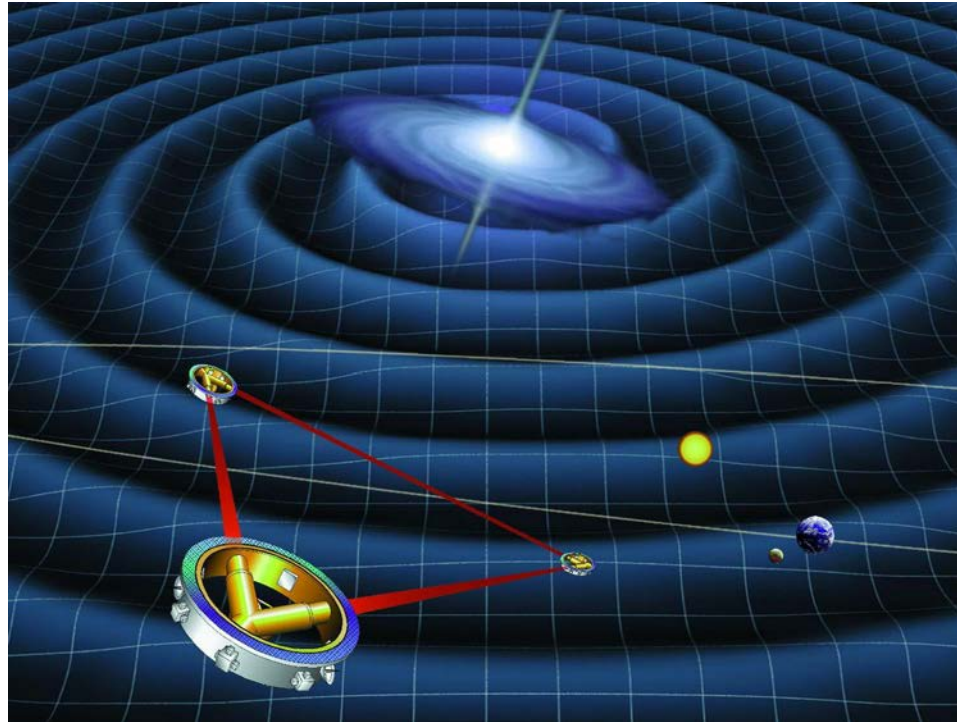
- Observations below 1 Hz
 - Observe evolution of systems
 - Sources not accessible to ground-based detectors
 - Earth's seismic noise dominates below few Hz
- More continuous sources at low frequencies.
- Observations at low frequencies benefit from larger detector arm lengths.



Observatories – complementary observations bands



LISA: Laser Interferometer Space Antenna

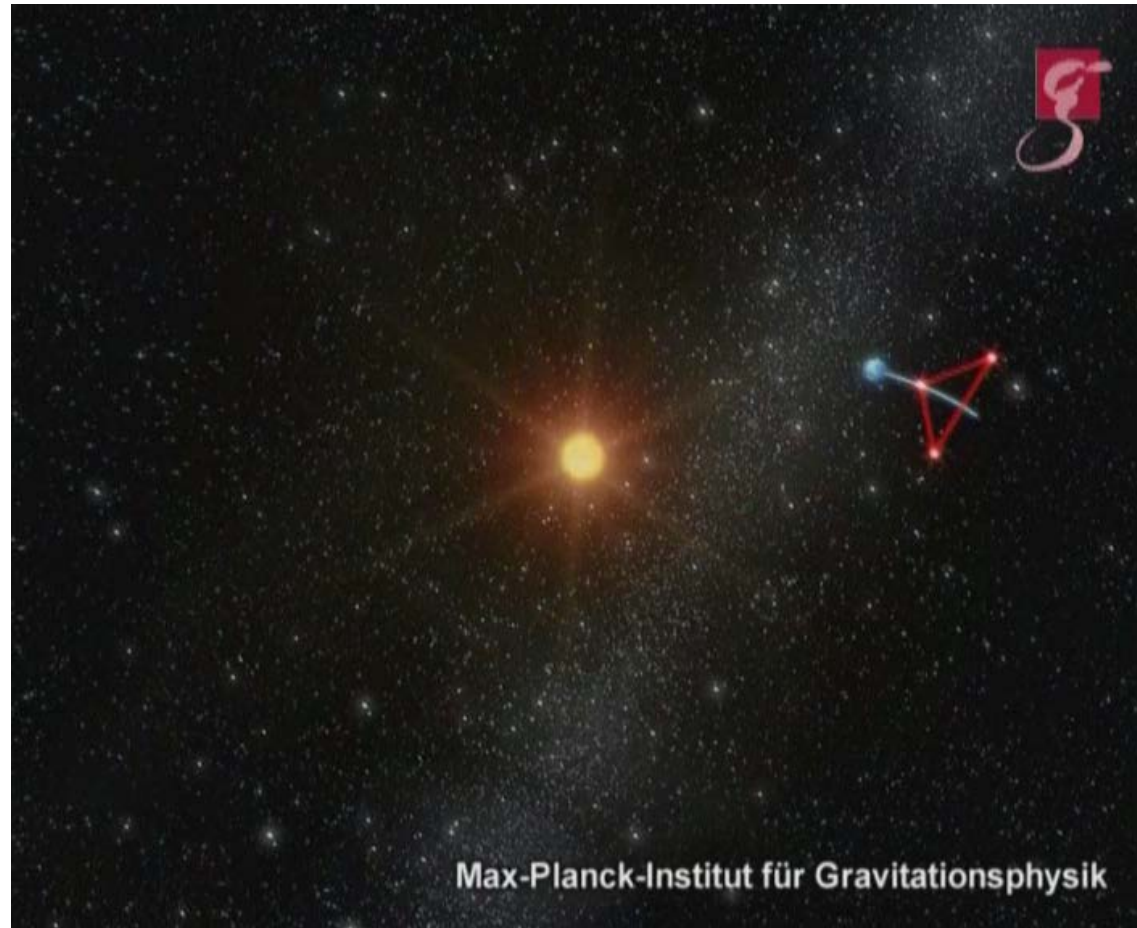


- Gravitational Wave Observatory in Space.
- Observation bandwidth: $10^{-4} - 10^{-1}$ Hz .
- Interferometer armlength: millions of km.
- Heliocentric orbit.



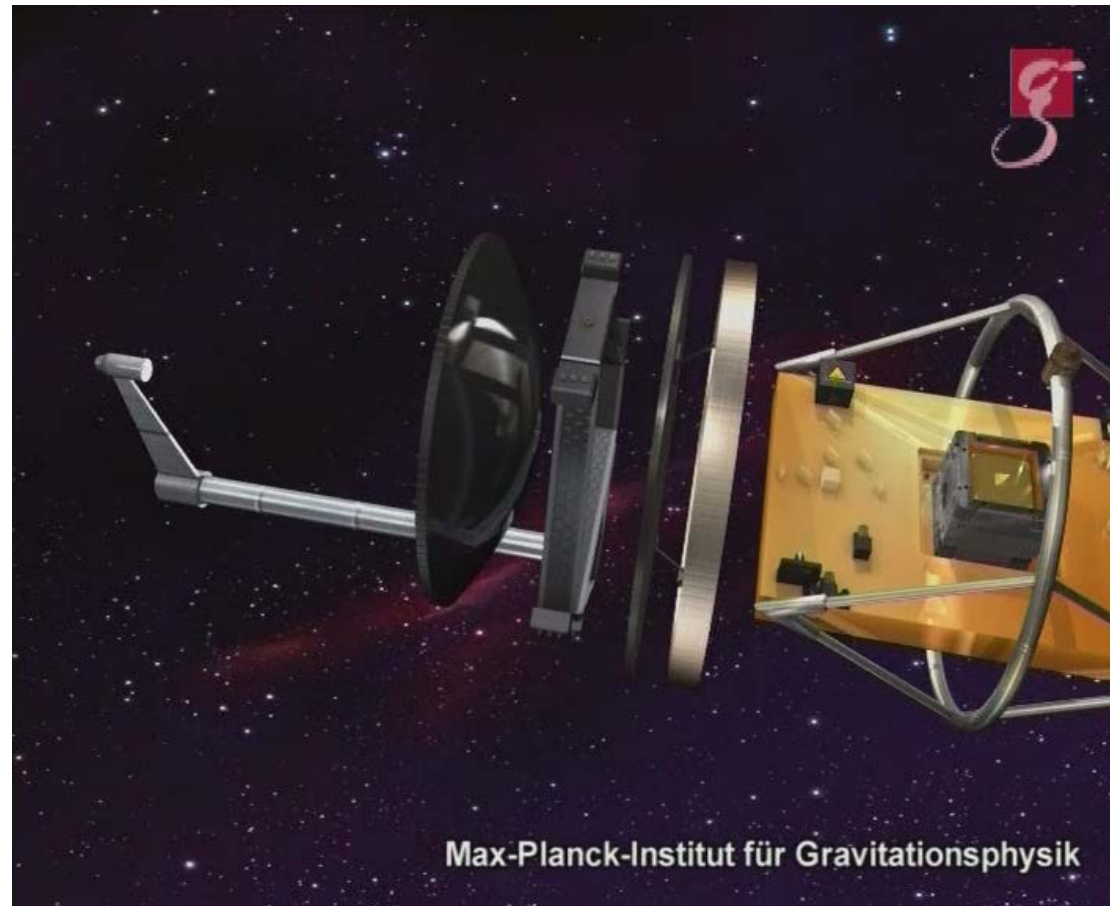
LISA Orbit

- Three spacecraft in quasi-equilateral triangle formation
- Trailing Earth around the Sun by approximately 20°
- Armlengths of few million km
+/- $\sim 1\%$



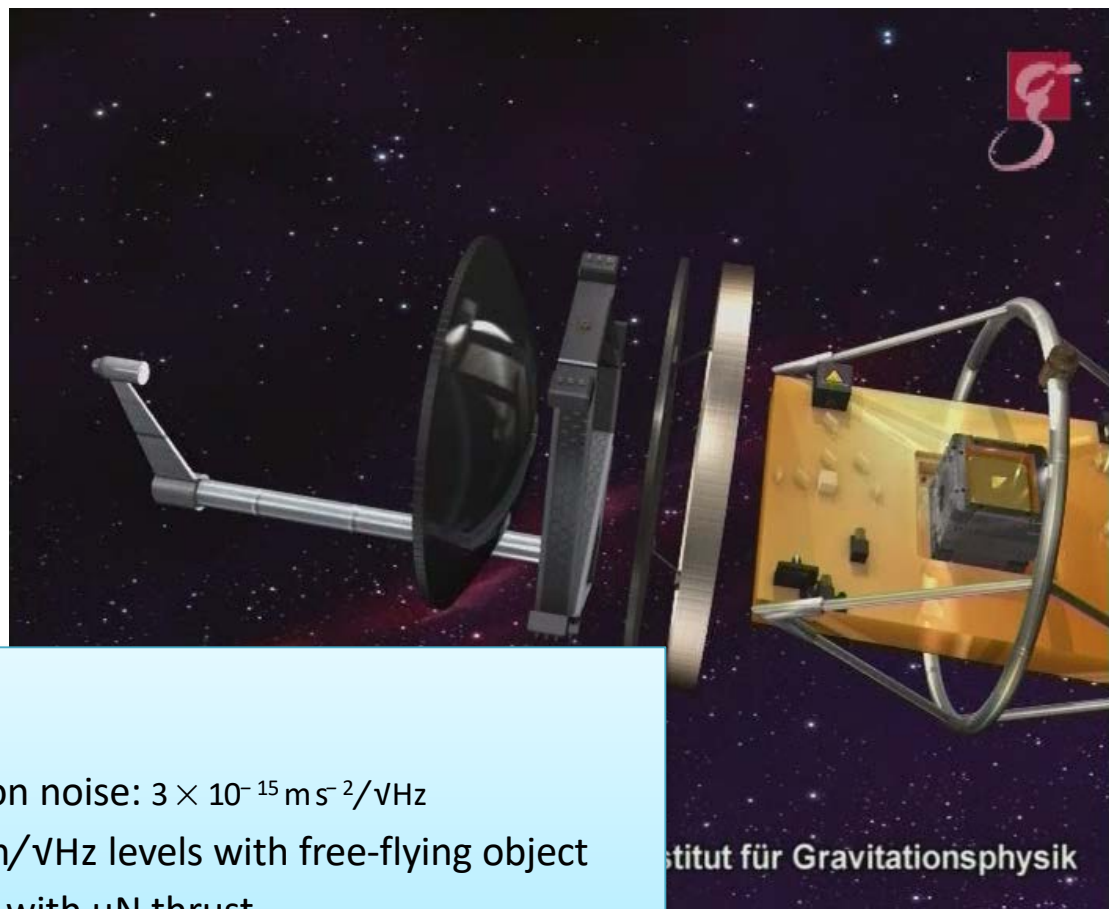
LISA optical bench and gravitational sensor

- Emitted beam:
 - ~40 cm diameter
 - 1 W optical power
- Received beam:
 - ~20 km diameter
 - 100 pW optical power



LISA optical bench and gravitational sensor

- Emitted beam:
 - ~40 cm diameter
 - 1 W optical power



- Received beam:
 - ~20 km diameter
 - 100 pW optical power

Challenges:

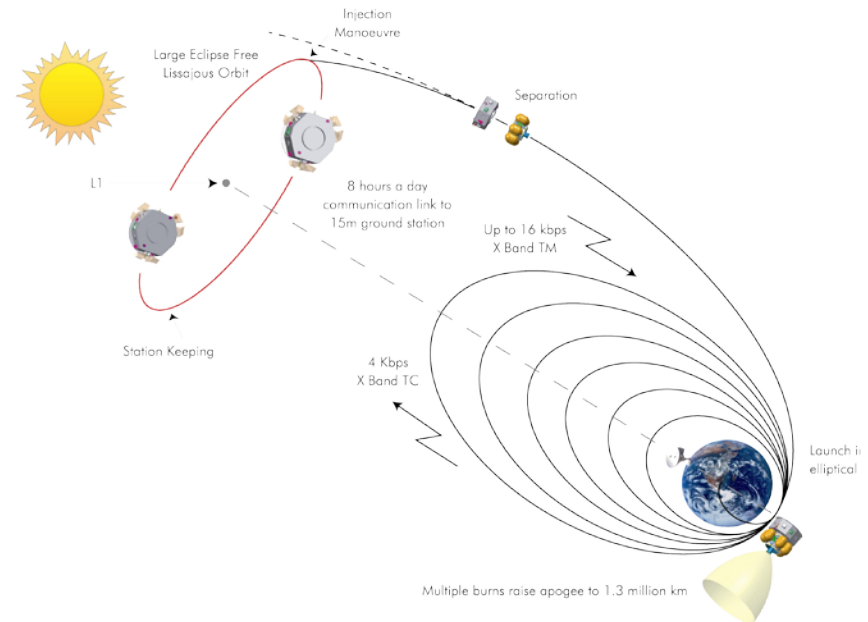
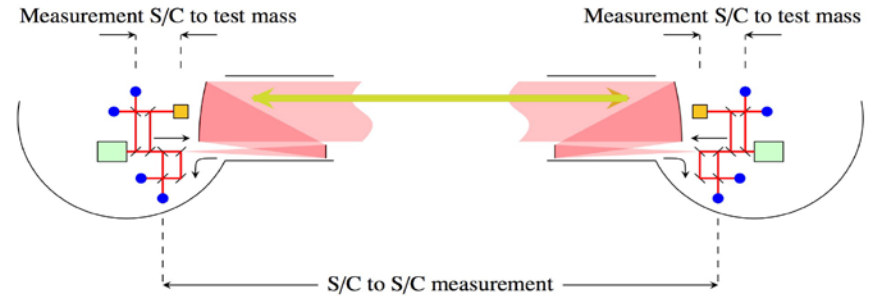
- Test mass acceleration noise: $3 \times 10^{-15} \text{ m s}^{-2} / \sqrt{\text{Hz}}$
- Interferometry at pm/ $\sqrt{\text{Hz}}$ levels with free-flying object
- Spacecraft actuators with μN thrust

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LISA Pathfinder

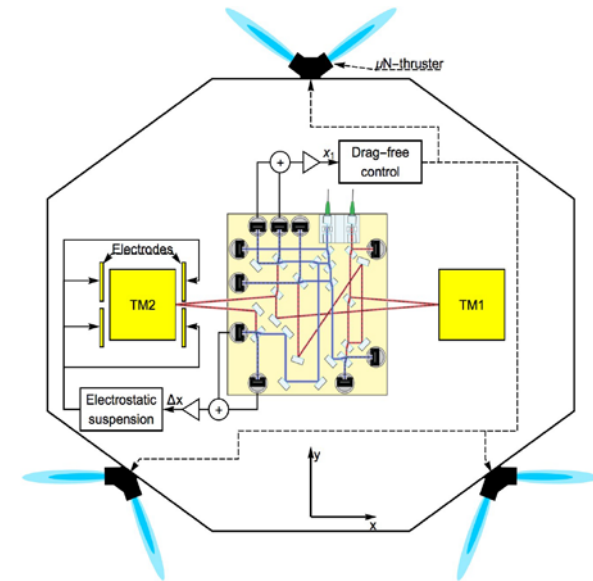
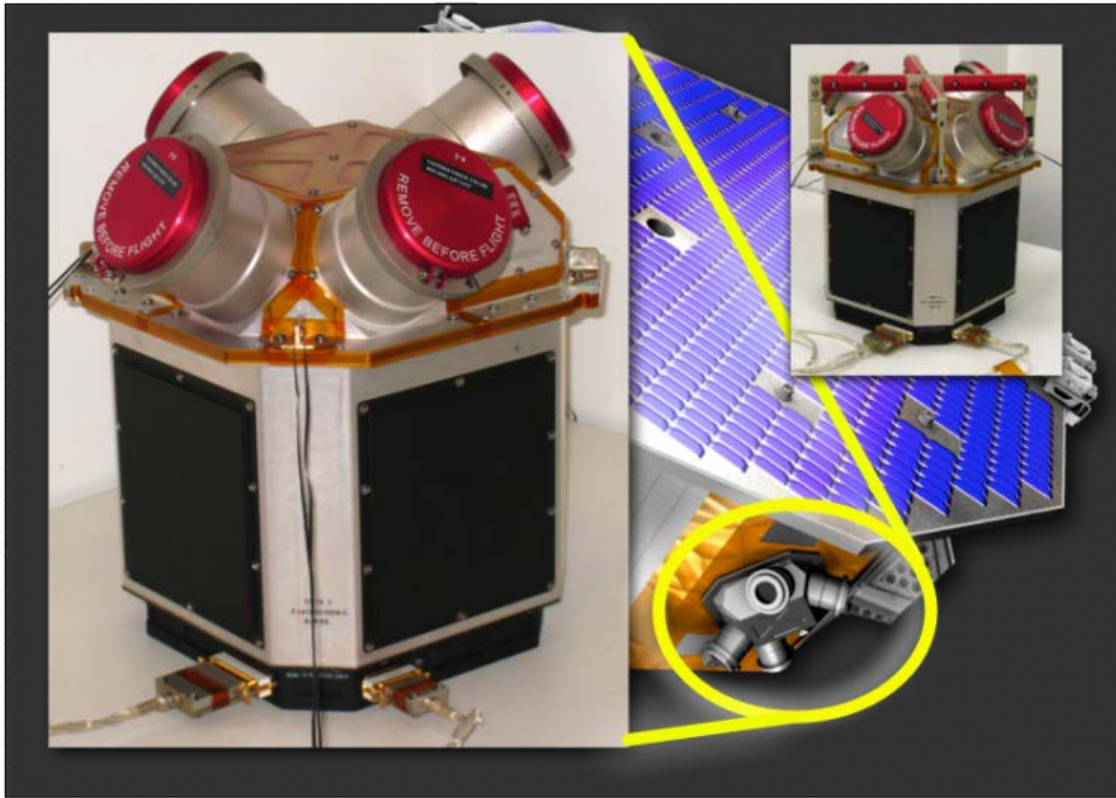


LISA Pathfinder

- Two LISA-like TMs inside one satellite
- ⇒ one small "LISA-arm":
- **Interferometry** between Test-Masses with **picometer** precision.
- **Drag Free** System for Test Masses with **femtonewton** stability.
- Micronewton thrusters for drag free control of the satellite.
- Two experiments:
 - One European – LTP
 - One American – DRS/ST7



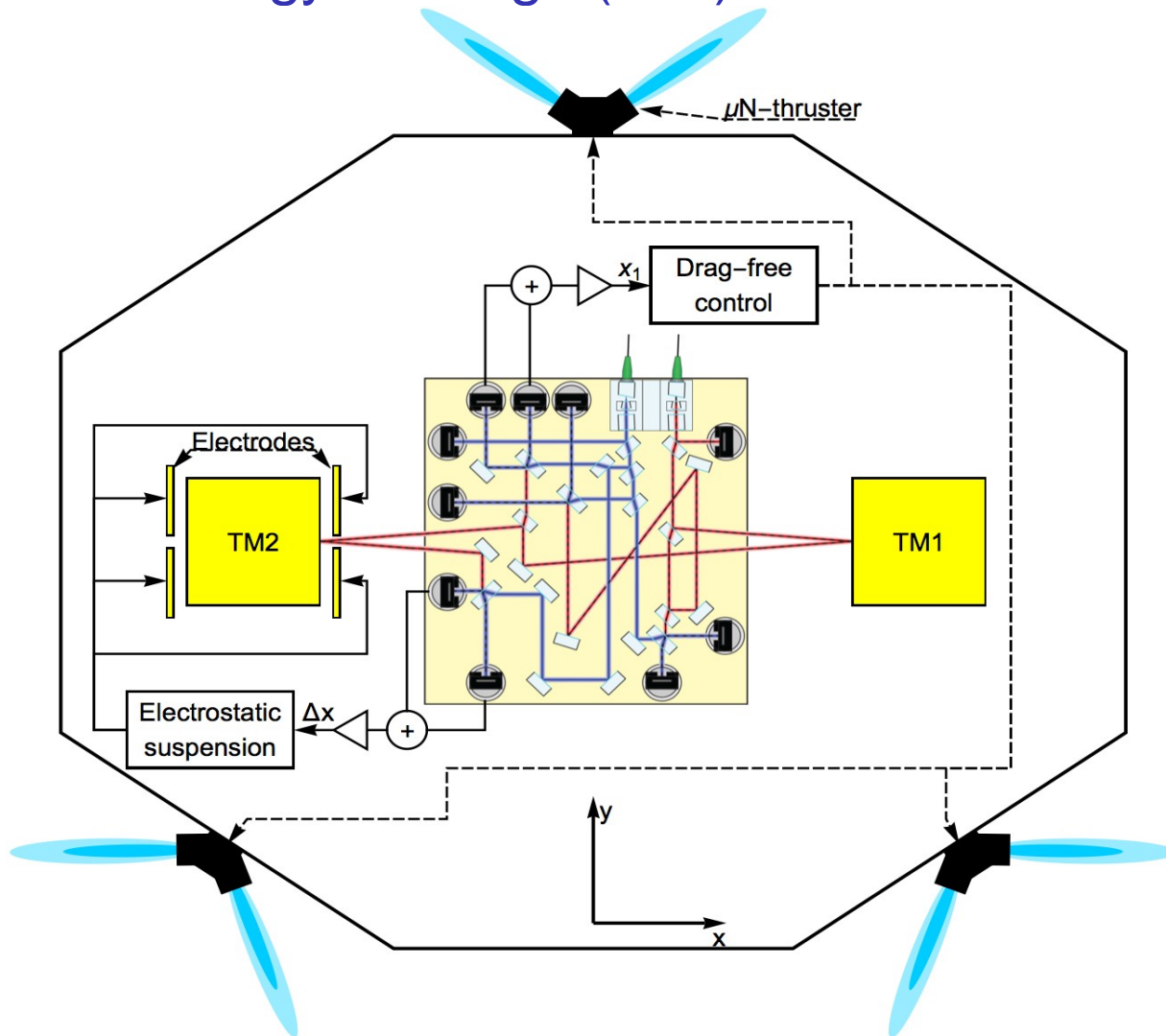
Disturbance Reduction System (DRS)



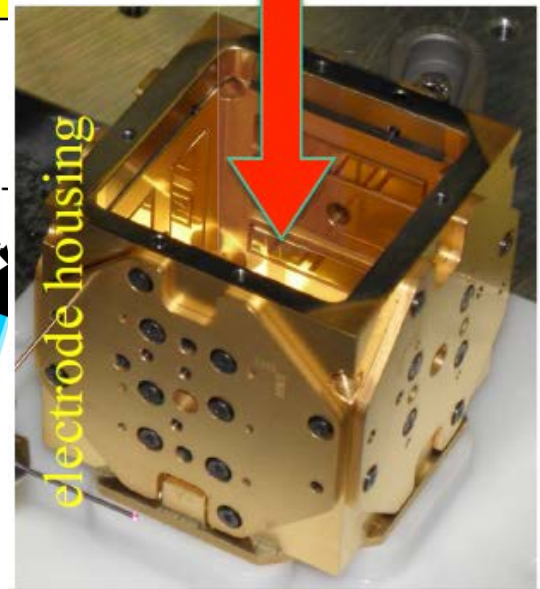
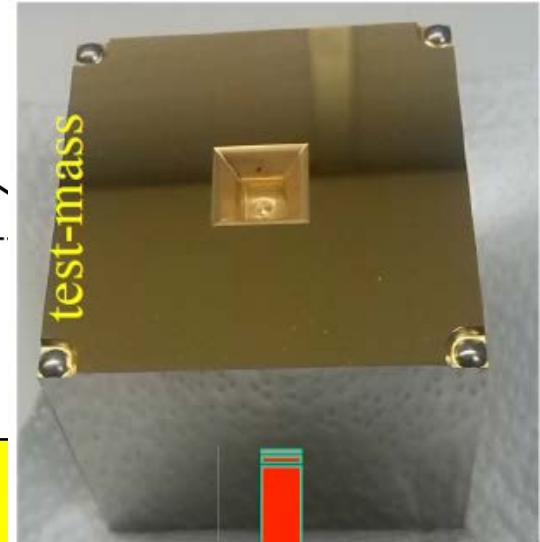
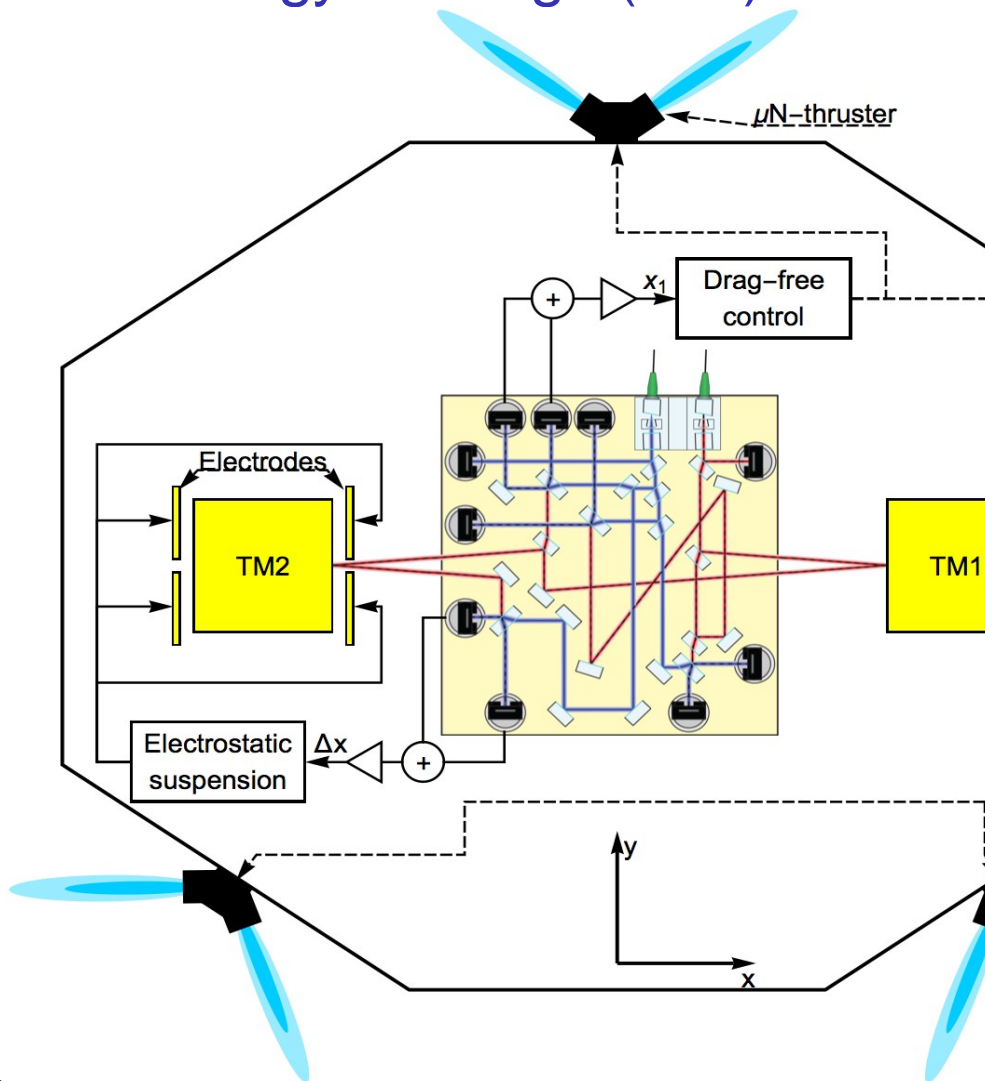
- Colloidal μN -thrusters
- Computer with control laws for drag-free



LISA Technology Package (LTP)



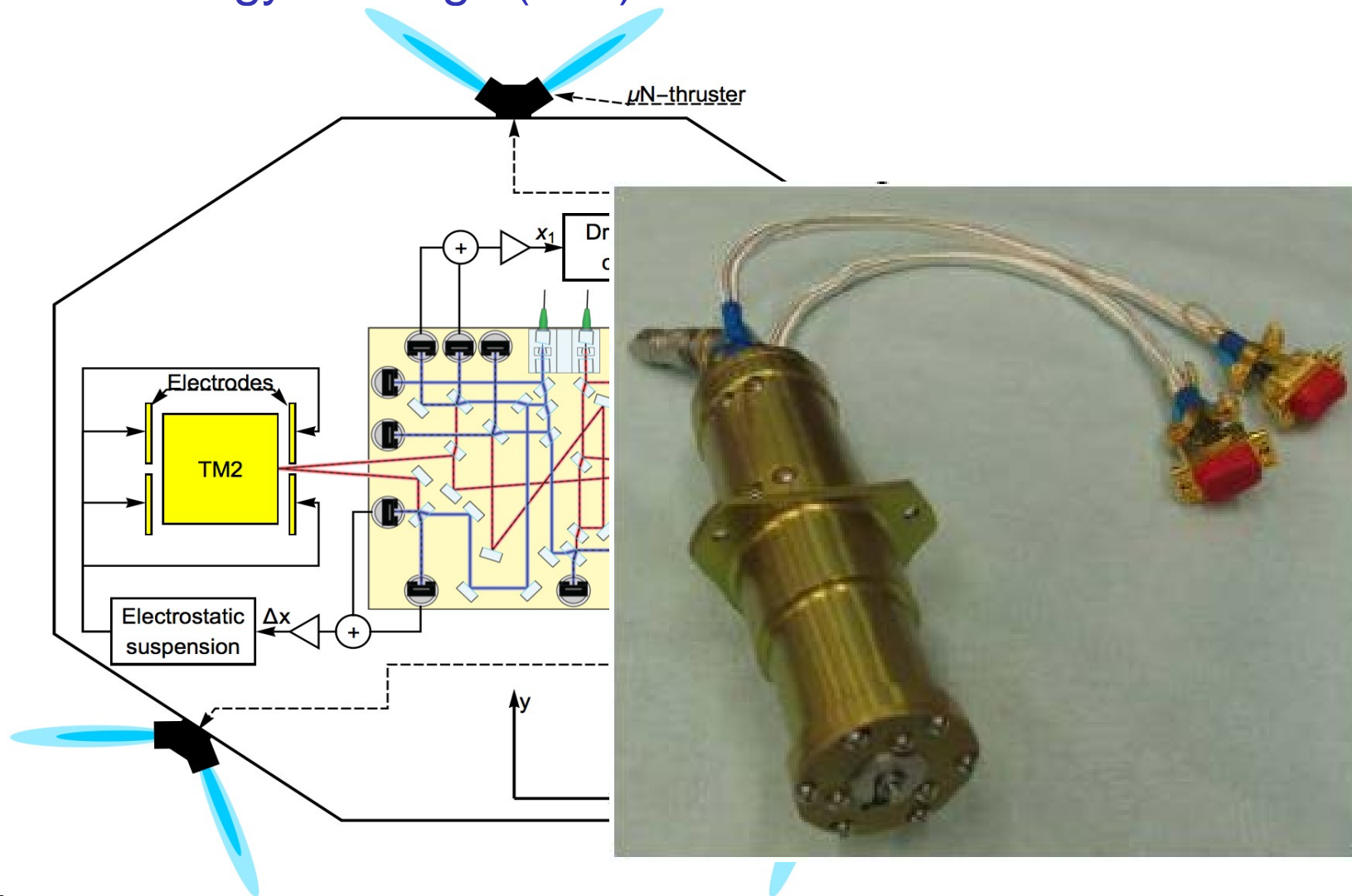
LISA Technology Package (LTP)



- Drag-free test masses.



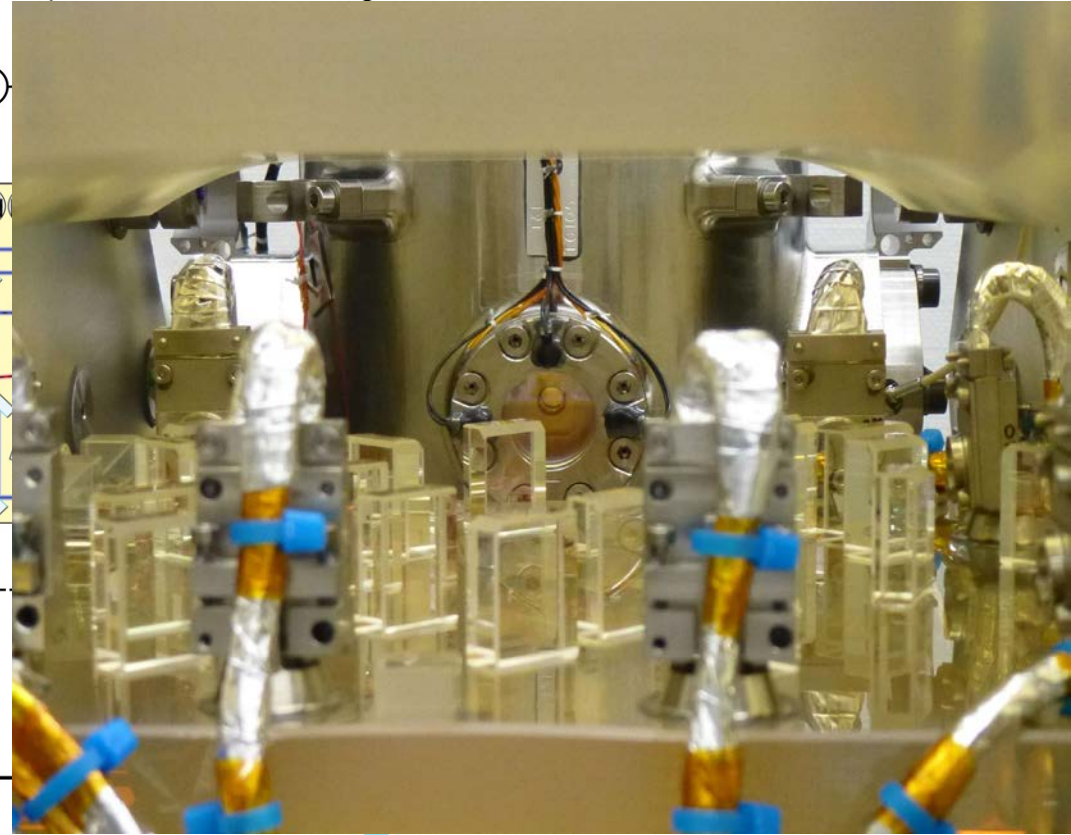
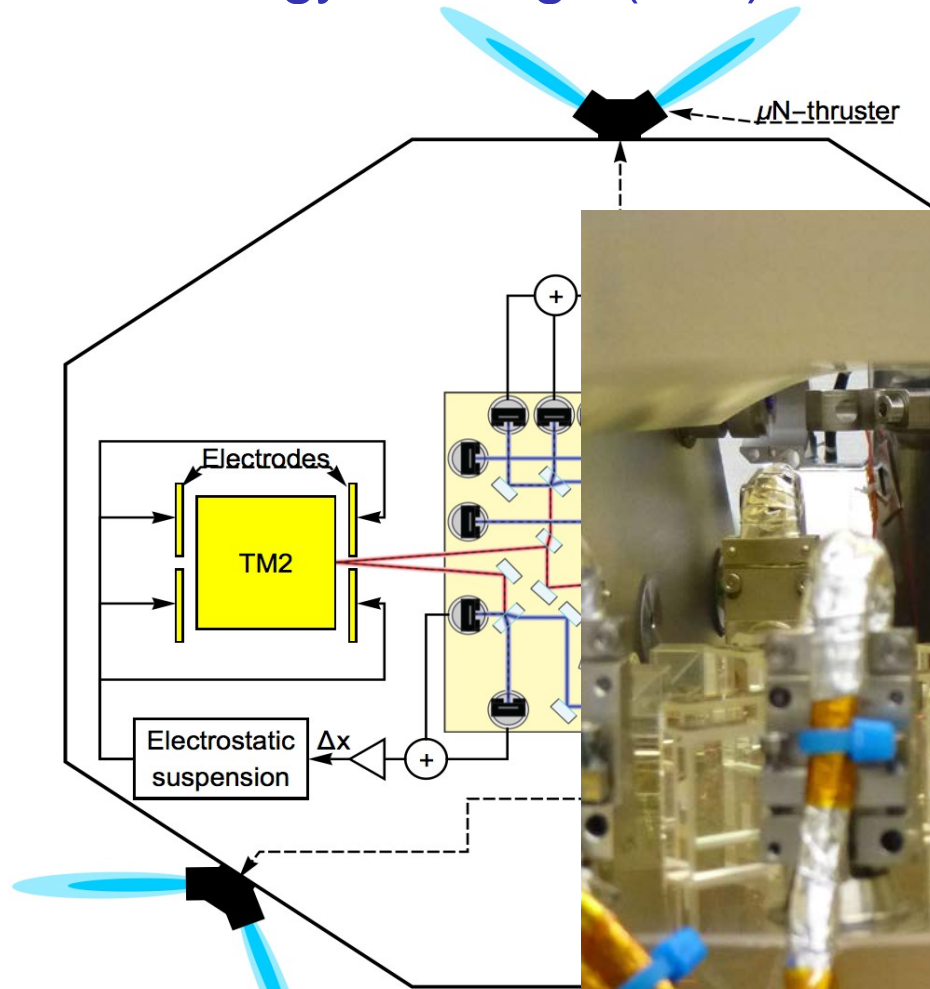
LISA Technology Package (LTP)



- Drag-free test masses.
- Cold gas (N_2) μN -thrusters.



LISA Technology Package (LTP)



- Drag-free test masses.
- Cold gas (N_2) μN -thrusters.
- Laser interferometers between free floating test masses.

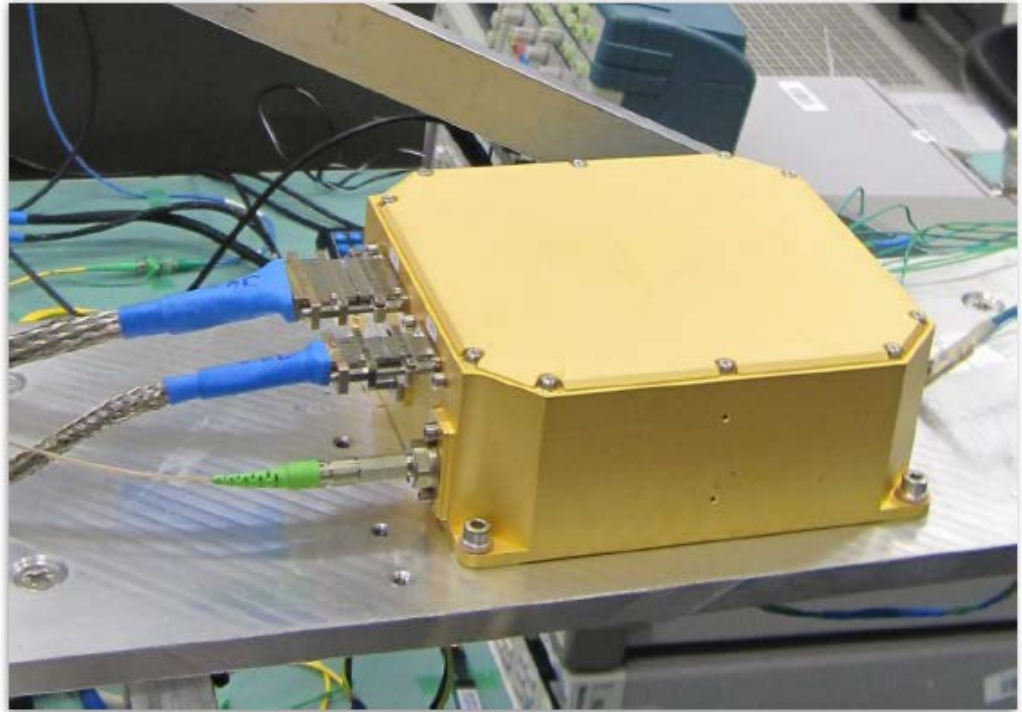


LTP Laser

Nd:YAG laser

λ : 1064 nm

Power: 45 mW

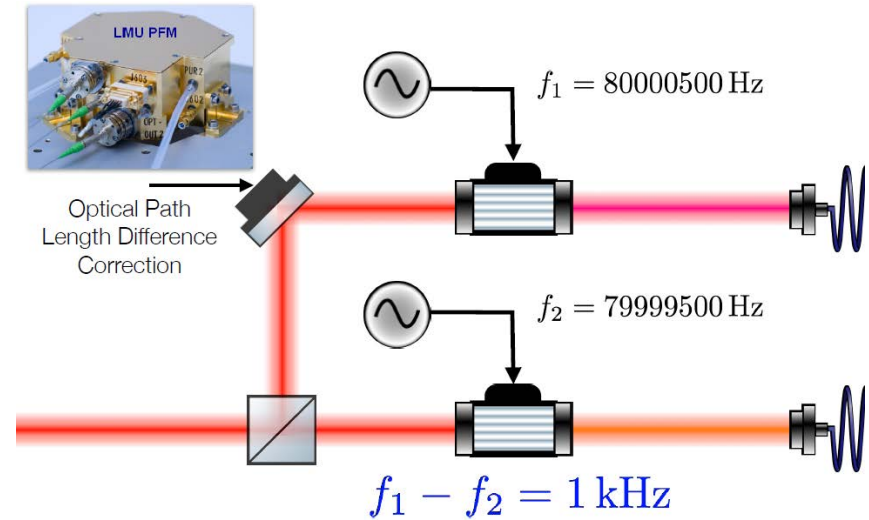


Operated at 38mW output power

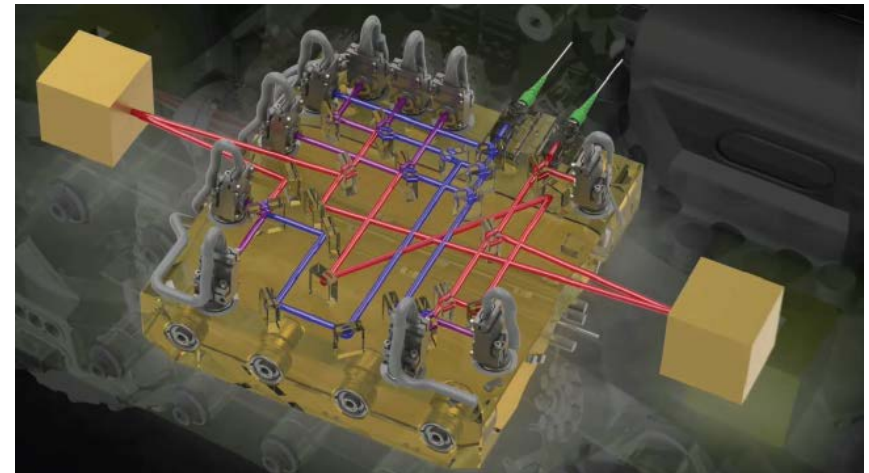


LISA Pathfinder Interferometry

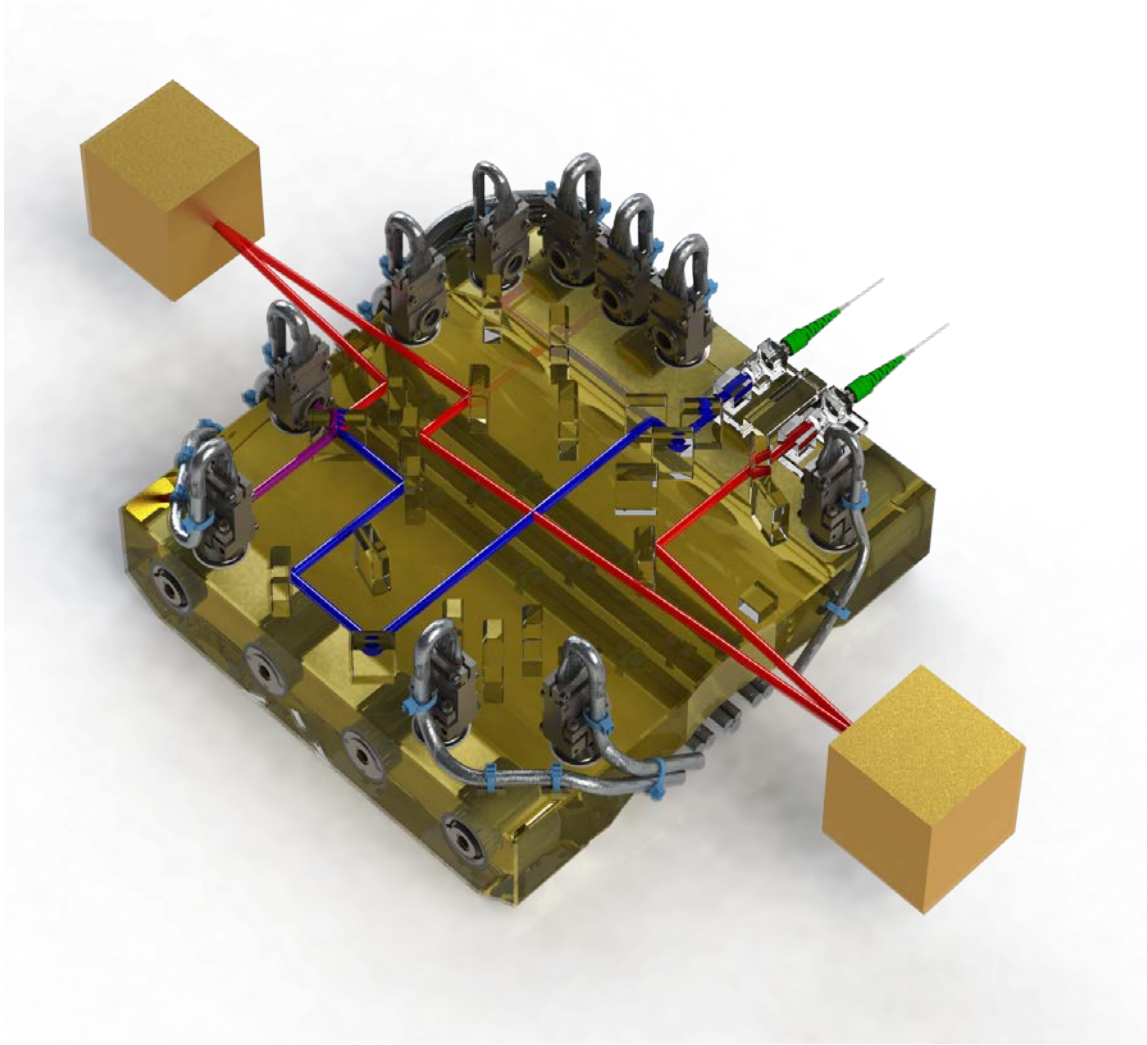
- Modulation Bench:
2 AOMs at nearly 80 MHz and
PZT phase actuators



- Optical bench:
Zerodur baseplate with 4 non-polarizing
Mach-Zehnder interferometers



LISA Pathfinder Interferometry

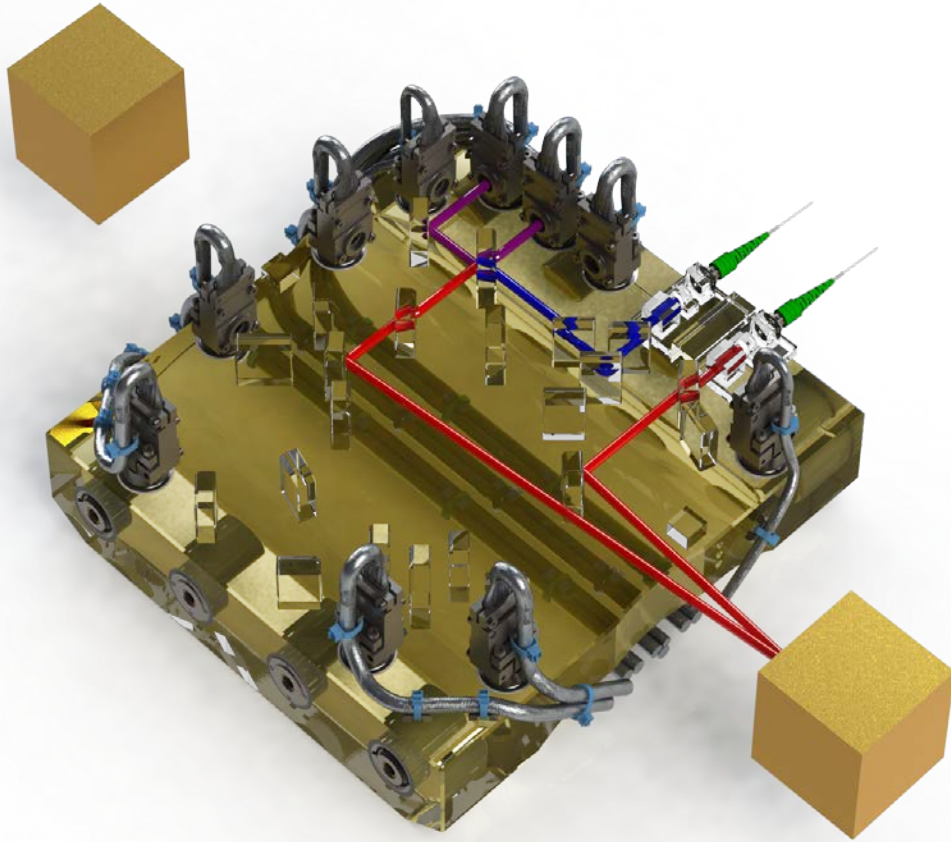


- X12 interferometer:

Measures relative separation and orientation between test masses.



LISA Pathfinder Interferometry

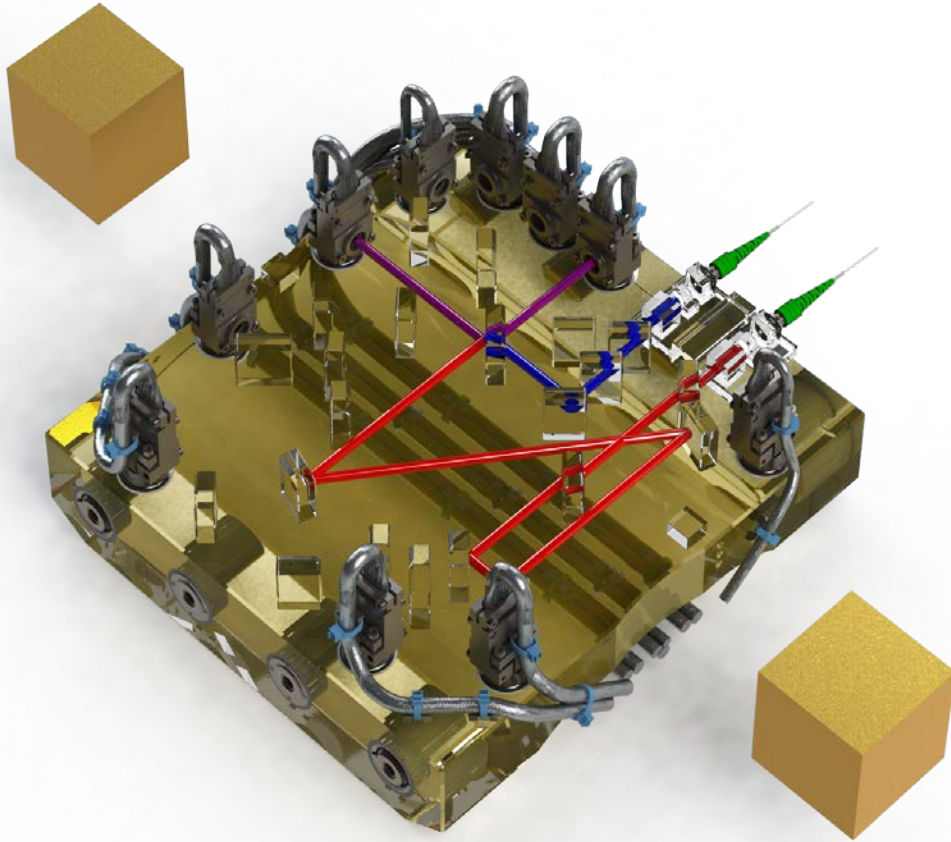


- X1 interferometer:

Measures displacement and orientation of test mass 1 wrt. optical bench.



LISA Pathfinder Interferometry

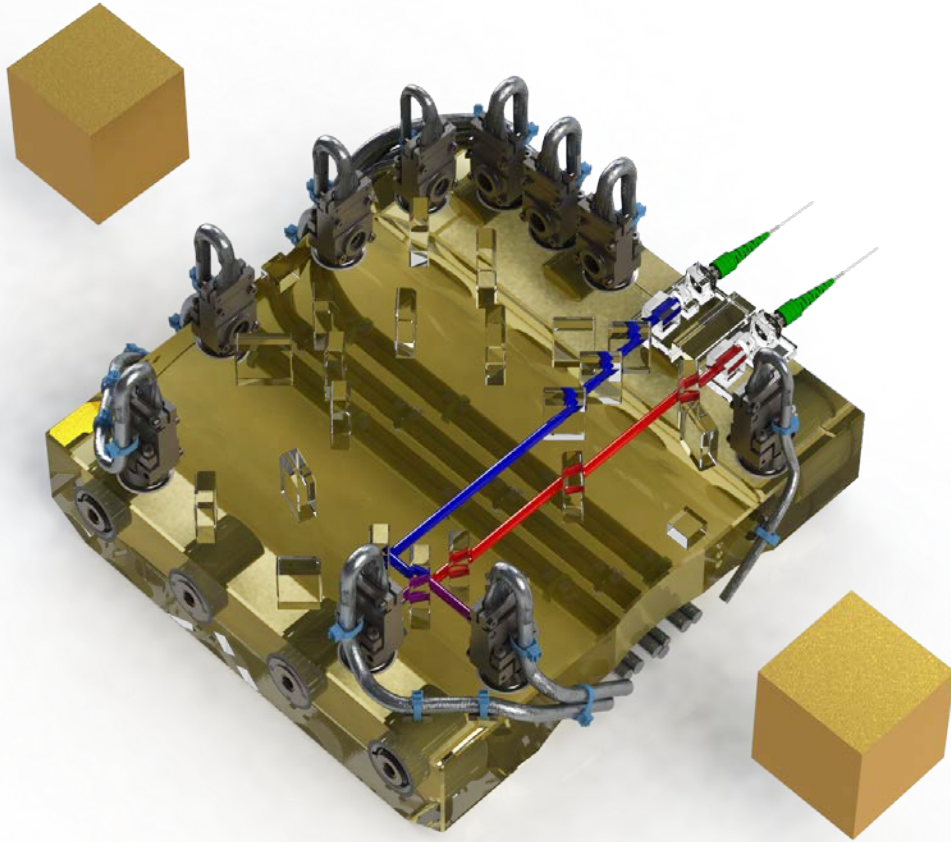


- Reference interferometer:

Measures common-mode noise from modulation bench and fibers to correct other interferometers.



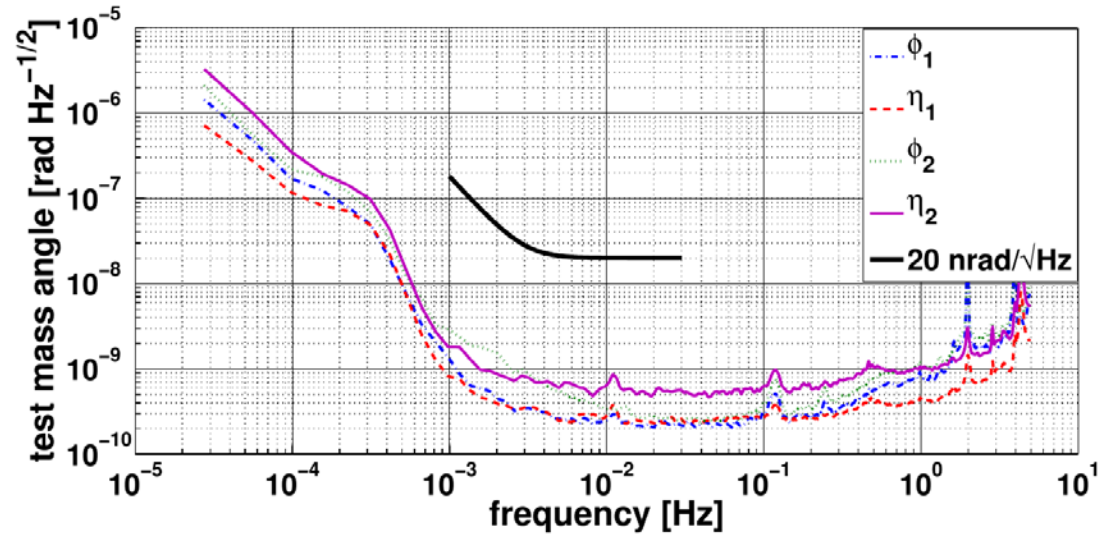
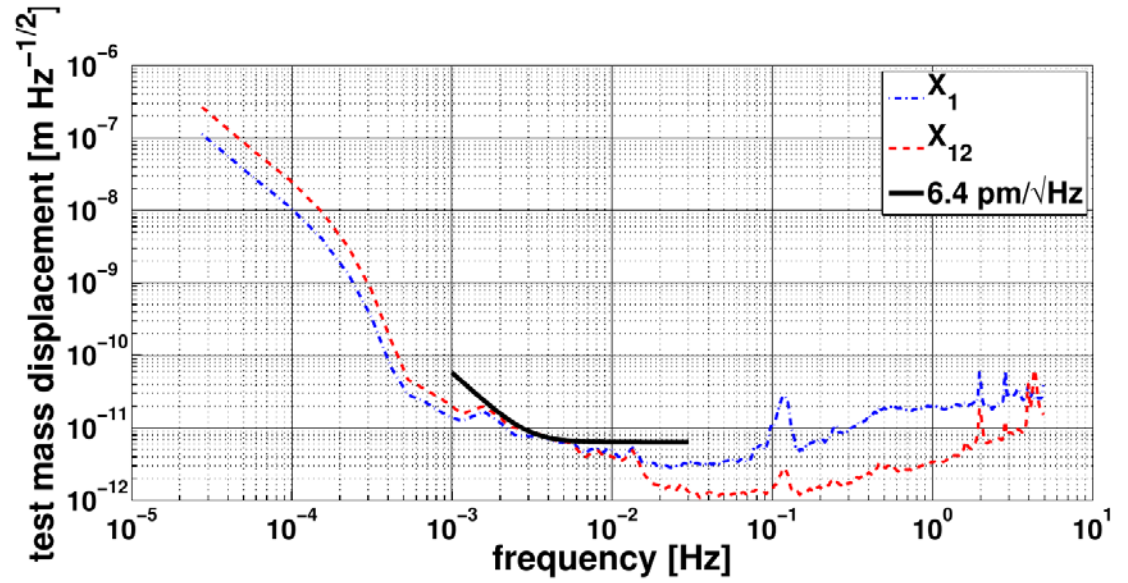
LISA Pathfinder Interferometry



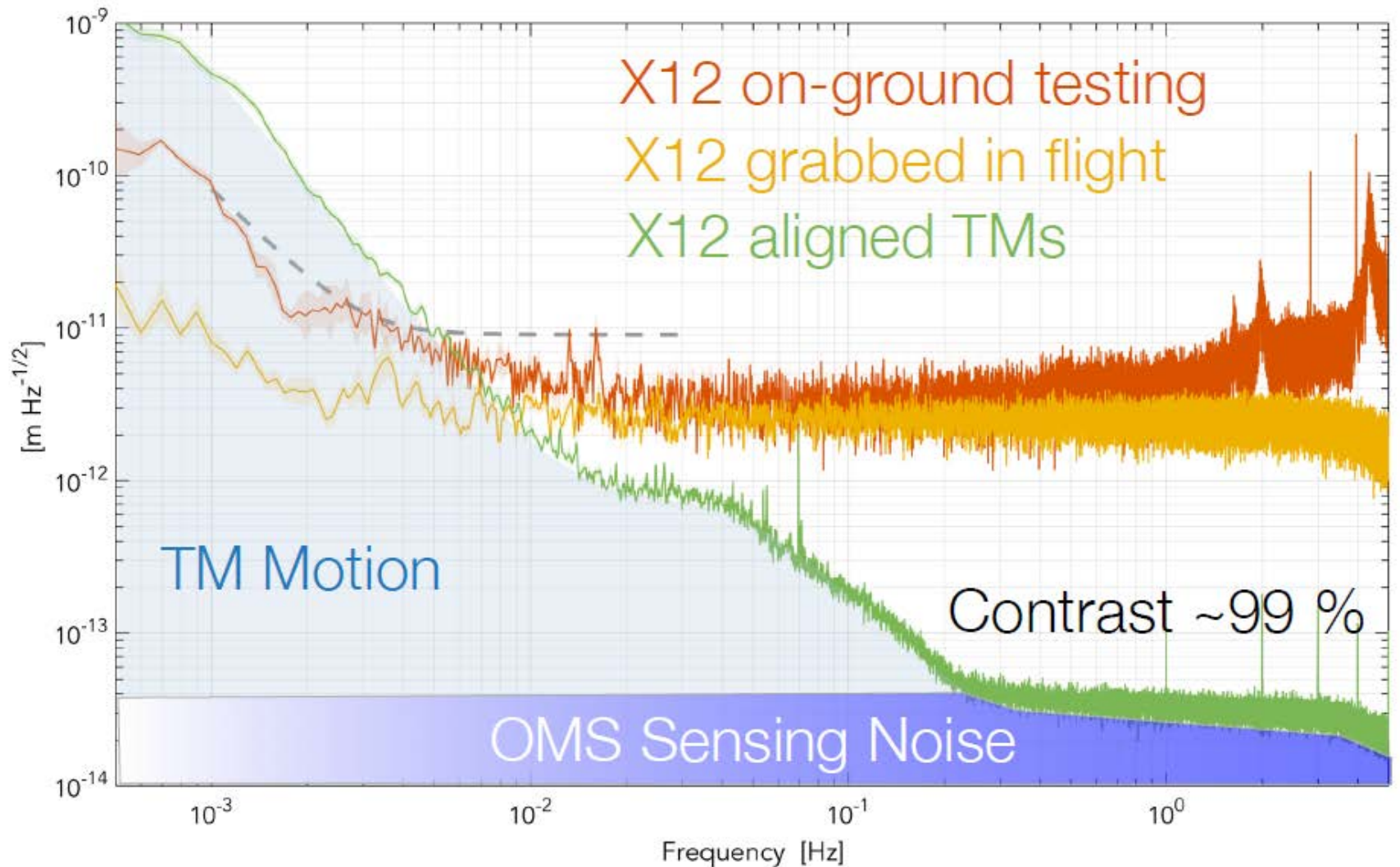
- Frequency interferometer:
Unequal arm lengths to measure the laser frequency noise and stabilize it.



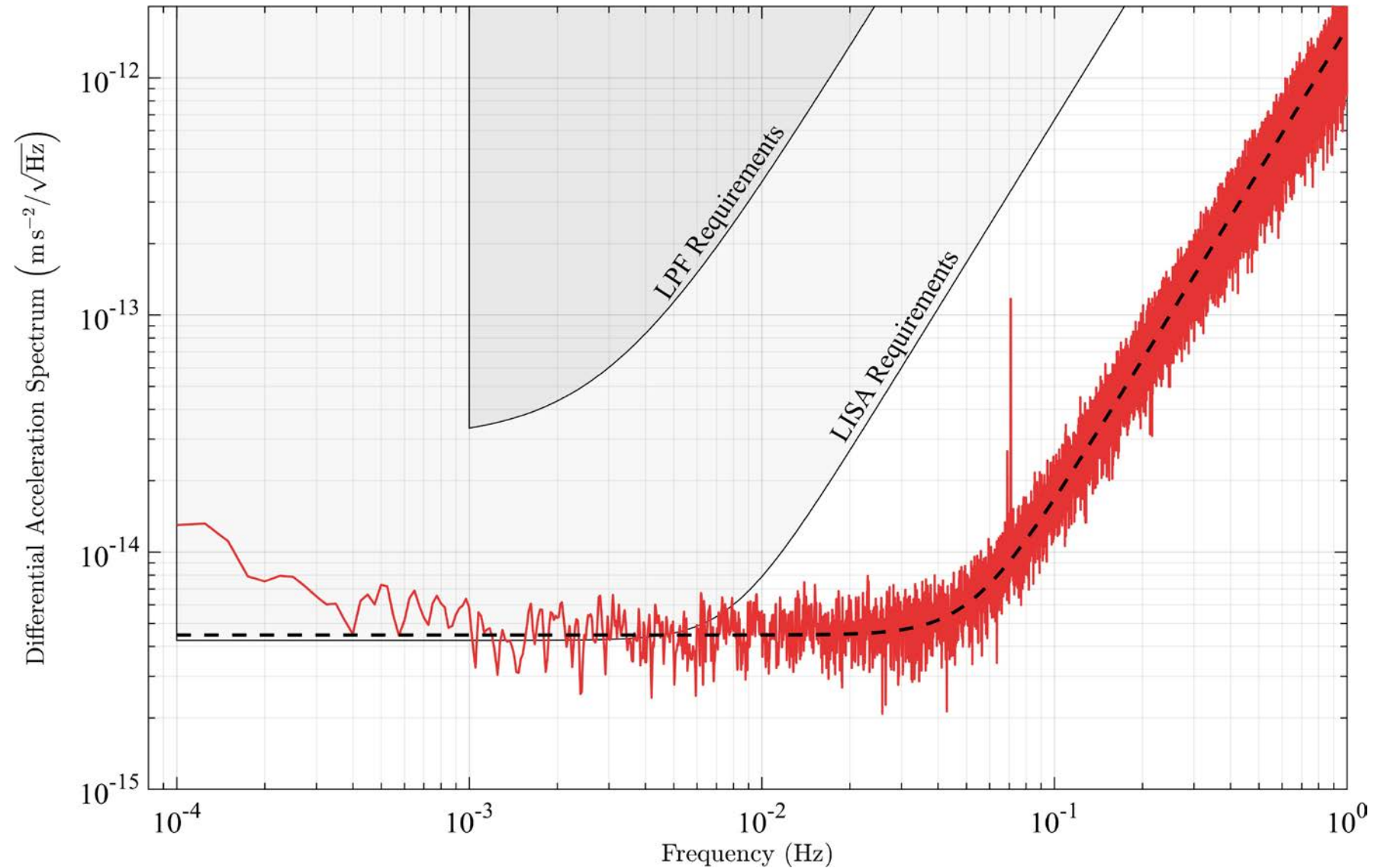
LISA Pathfinder Interferometry – Performance on ground



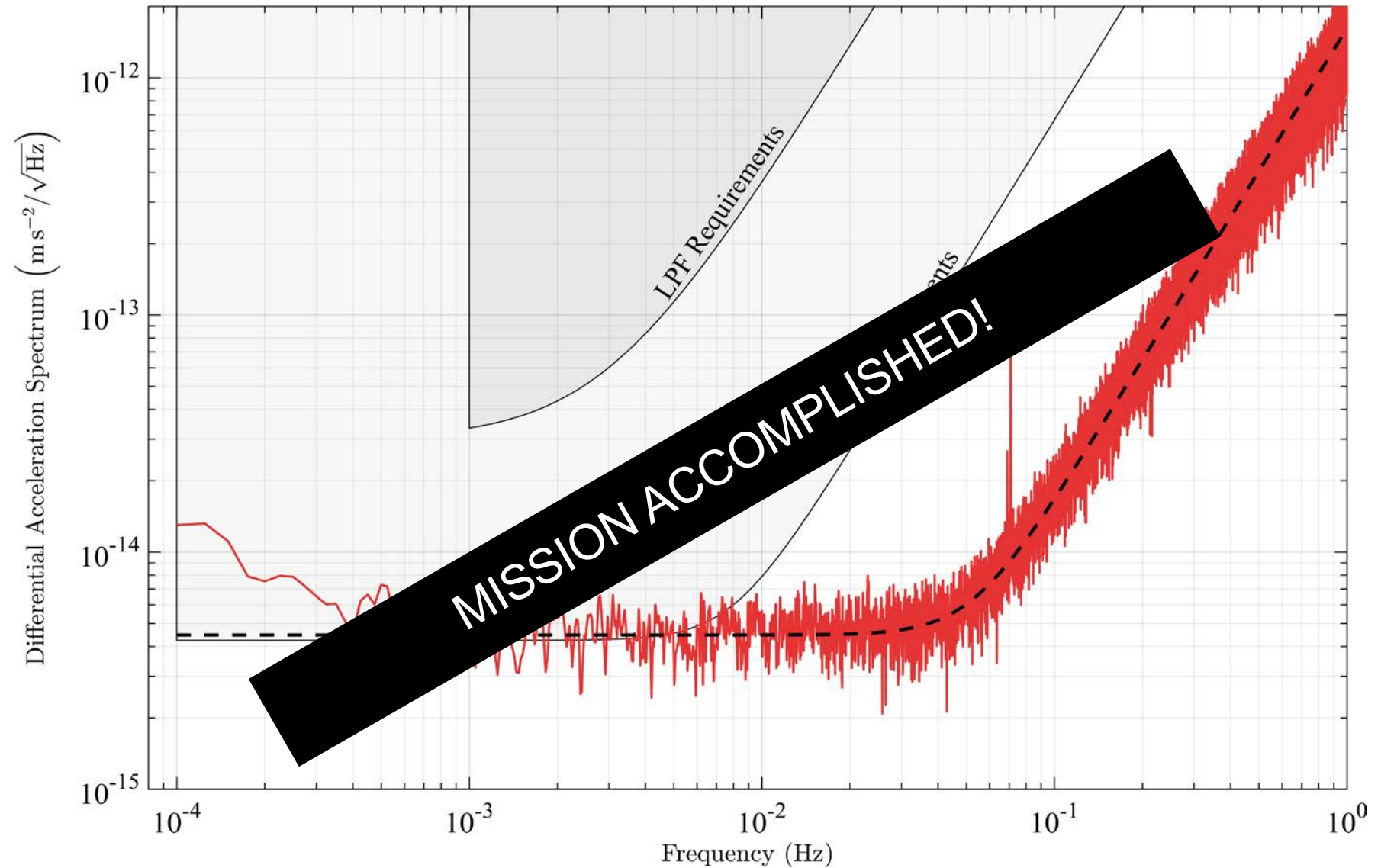
LISA Pathfinder Interferometry – Performance in orbit



LISA Pathfinder Interferometry – Performance in orbit



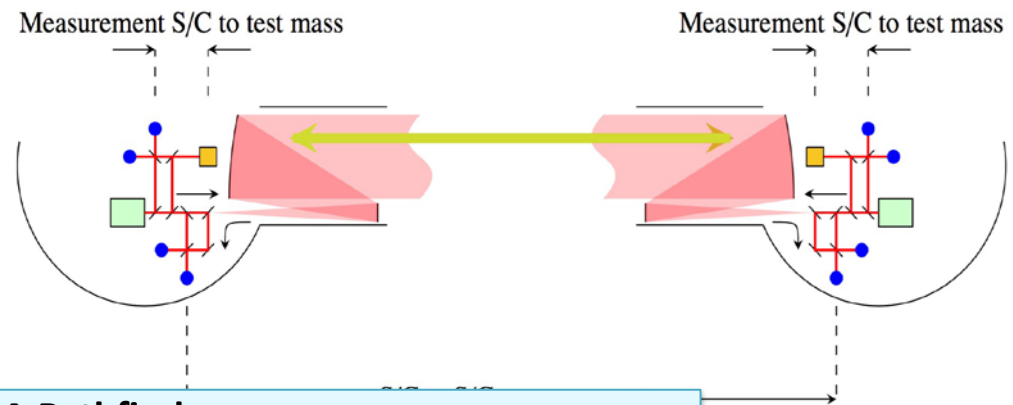
LISA Pathfinder Interferometry – Performance in orbit



LISA Pathfinder

- Two LISA-like TMs inside one satellite
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- ✓ **Interferometry** between Test-Masses with **picometer** precision.
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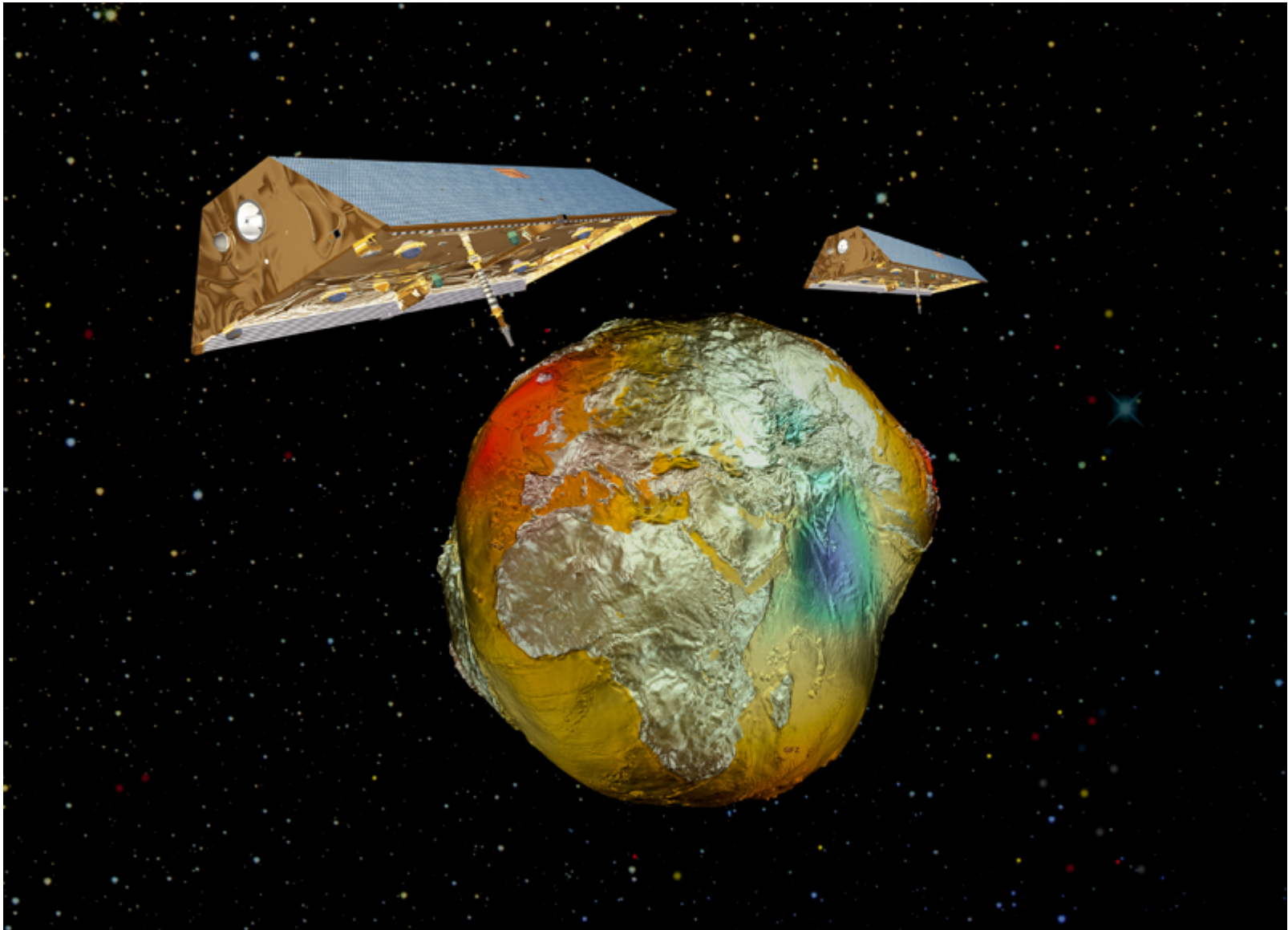
LISA relevant aspects not tested in LISA Pathfinder:

- Two
 - Long baseline intersatellite laser interferometry with low power
 - μ -Cycle phase measurement with a continuously doppler shifting beat note
 - Constellation acquisition

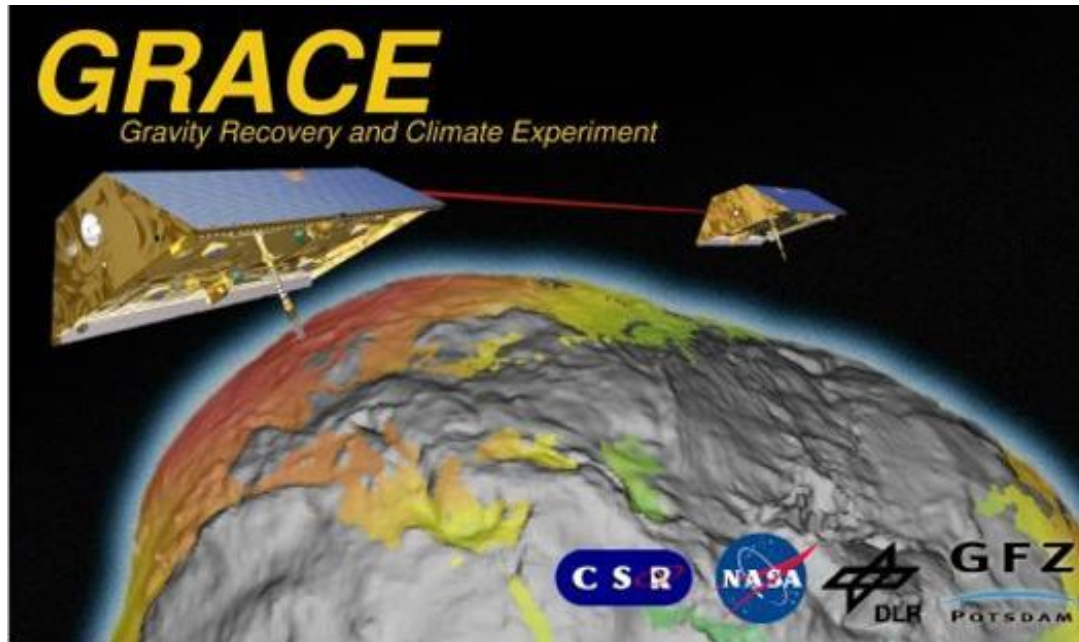
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GRACE follow-on



GRACE: Gravity Recovery and Climate Experiment



GRACE: Gravity Recovery and Climate Experiment



- GRACE was launched in 2002.
- Nominal orbit: 483 – 508 km, separation: 200 km
- Originally designed for 5 year nominal lifetime.
- Since 2012 in slowly decaying orbit:
 - currently at approximately 350 km



GRACE: Gravity Recovery and Climate Experiment



- GRACE was launched
- Nominal orbit: 480 km
- Originally designed for 5 years
- Since 2012 in slow decay orbit
 - currently at a



GRACE follow-on

- Planned launch date: December 2017
- Nearly identical to GRACE
 - Main focus is to provide continuity of data to science community.
 - Minor improvements:
 - Star trackers
 - Slightly better accelerometers
- Laser ranging interferometer
 - Technology demonstration payload
 - Race-track configuration
 - Similarities to LISA:
 - Received optical power: ~ 100 pW
 - Doppler shifting beat note
 - Laser frequency stability
(first LISA stage)



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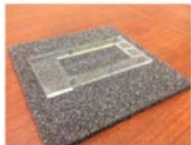


HOWEVER: required sensitivity is a few orders of magnitude less demanding than LISA.

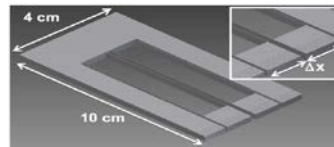


Novel optomechanical technologies for gravitational physics and inertial sensing

Gravimeters & Gradiometers

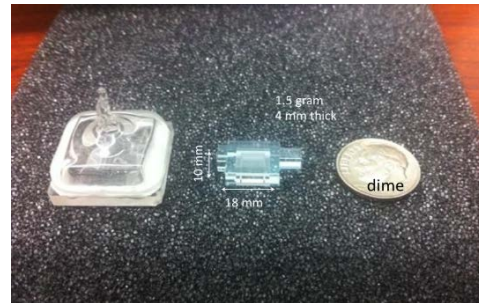
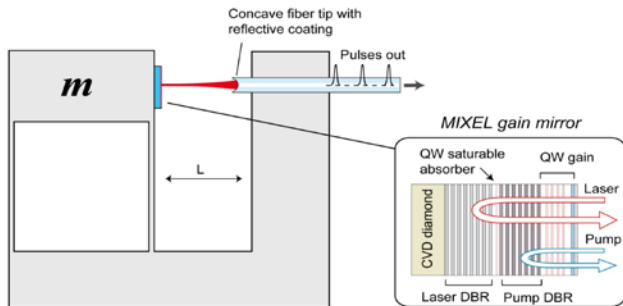


$f_0 = 10\text{ Hz}$
 $m = 1000\text{ mg}$

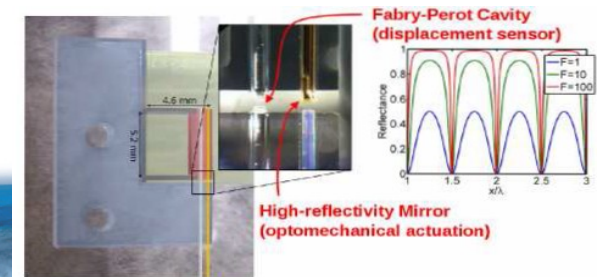


Micro-optical motion sensors

An Optomechanical Laser



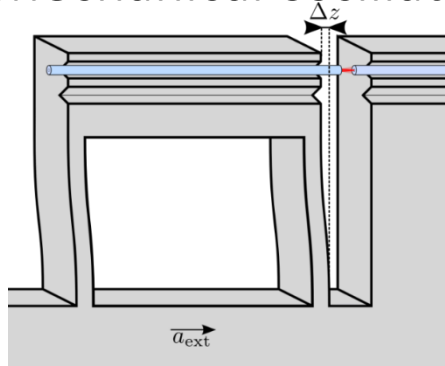
Self-referenced force sensors



Knowledge for Tomorrow

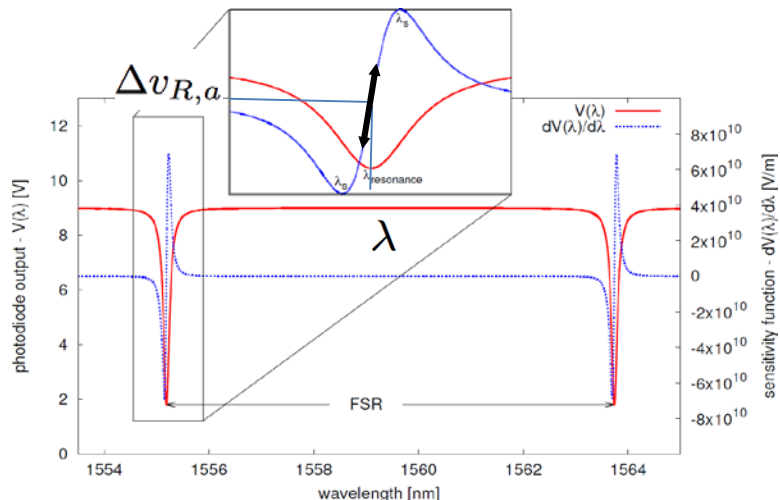
Optomechanical accelerometer concept

▶ Mechanical oscillator



- Acceleration \rightarrow test mass displacement Δz_m
- Linear uniaxial motion $\frac{\Delta z(\omega)}{a_{\text{ext}}(\omega)} = -\frac{1}{\omega_0^2 - \omega^2 + i\frac{\omega_0}{Q}\omega}$
 - Two parameters:
 - natural frequency ω_0
 - mechanical quality factor Q
 - SI frequency standard traceability
- Optical length changes \rightarrow reflected power changes

▶ Fabry-Pérot cavity



- Absolute optical length measurement:
Free Spectral Range (FSR): distance between resonances

$$L = \frac{c}{2 \text{FSR}}$$

- Linearization:

$$\Delta v_{R,a} = \frac{\lambda_0}{\bar{z}_m} \left(\frac{dv}{d\lambda} \right) \Delta z_m$$

- Three parameters:
 - cavity length \bar{z}_m
 - laser wavelength λ_0
 - derivative of reflectivity wrt. wavelength $\frac{dR}{d\lambda}$
- SI wavelength standard traceability

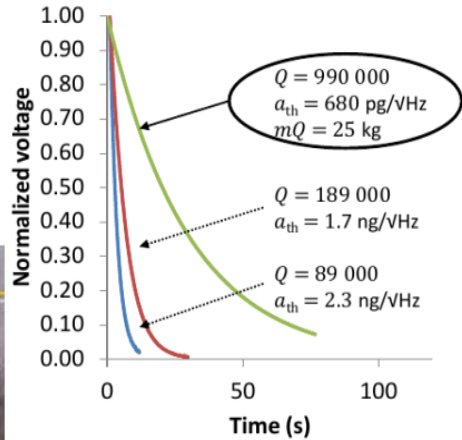
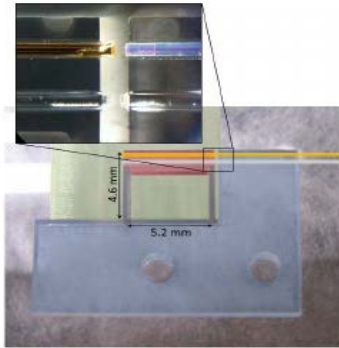


Optomechanical accelerometer prototype

Mechanical oscillator – Q measured: 4×10^6

- Monolithic fused-silica flexure
 - $\omega_0 = 2\pi \times 10.7$ kHz
 - $m = 25$ mg

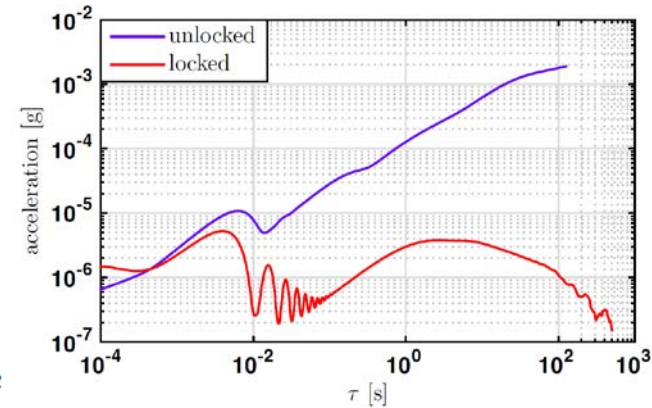
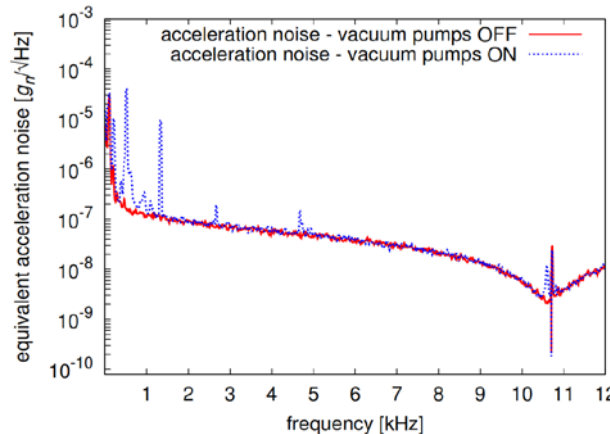
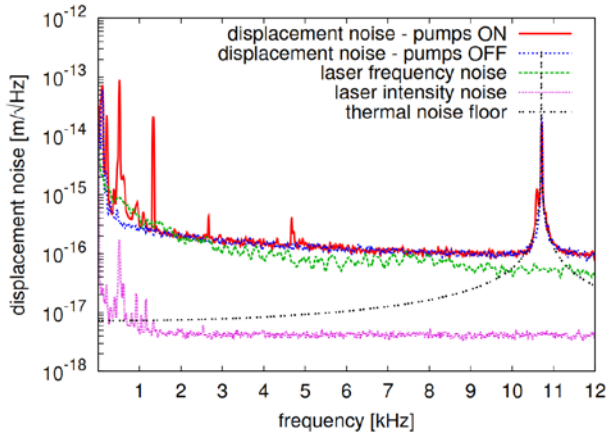
$Q \approx 10^6$
 $a_{th} = 680$ pg/VHz



displacement resolution: 10^{-16} m/VHz

acceleration resolution: < 100 ng/VHz

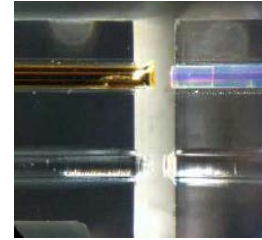
Allan variance - $10^{-5}g$ over 100s



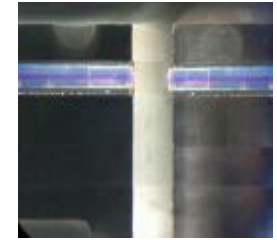
Optical sensor

- Fabry-Pérot fiber micro-cavities of low and high finesse
- Cavity lengths of 40-200 μ m | FSR at THz frequencies

low finesse: 2-100



high finesse: > 1500

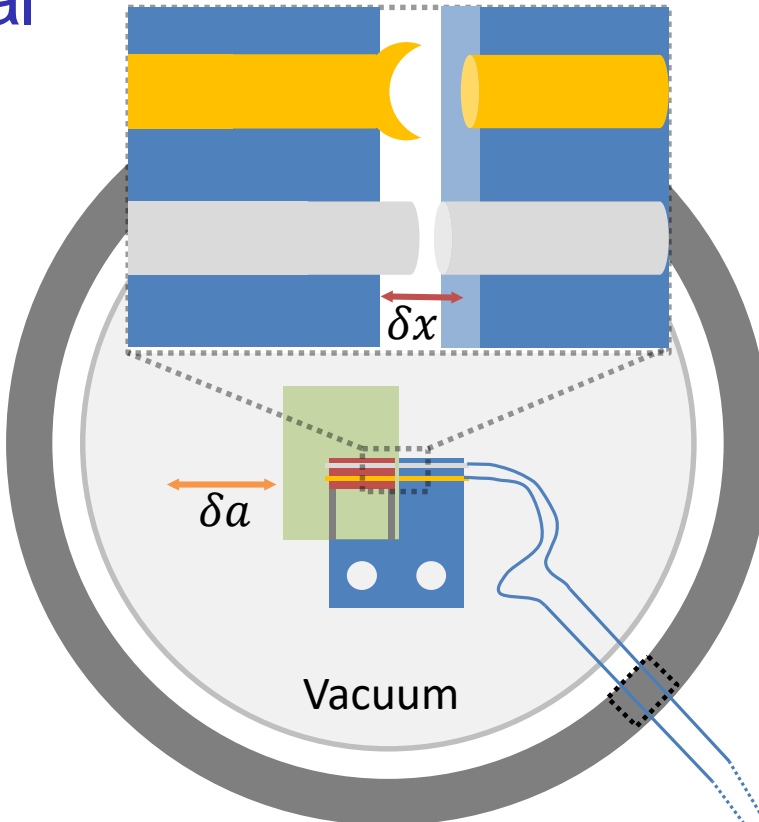
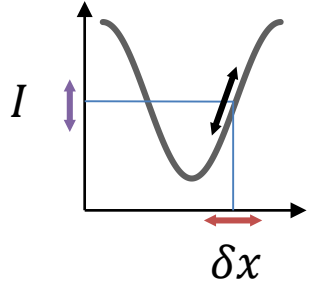


- plano-plano uncoated flatly cleaved fibers
- plano-concave dielectric and metalized fiber mirrors
- plano and laser-ablated concave fiber mirrors with HR dielectric coatings

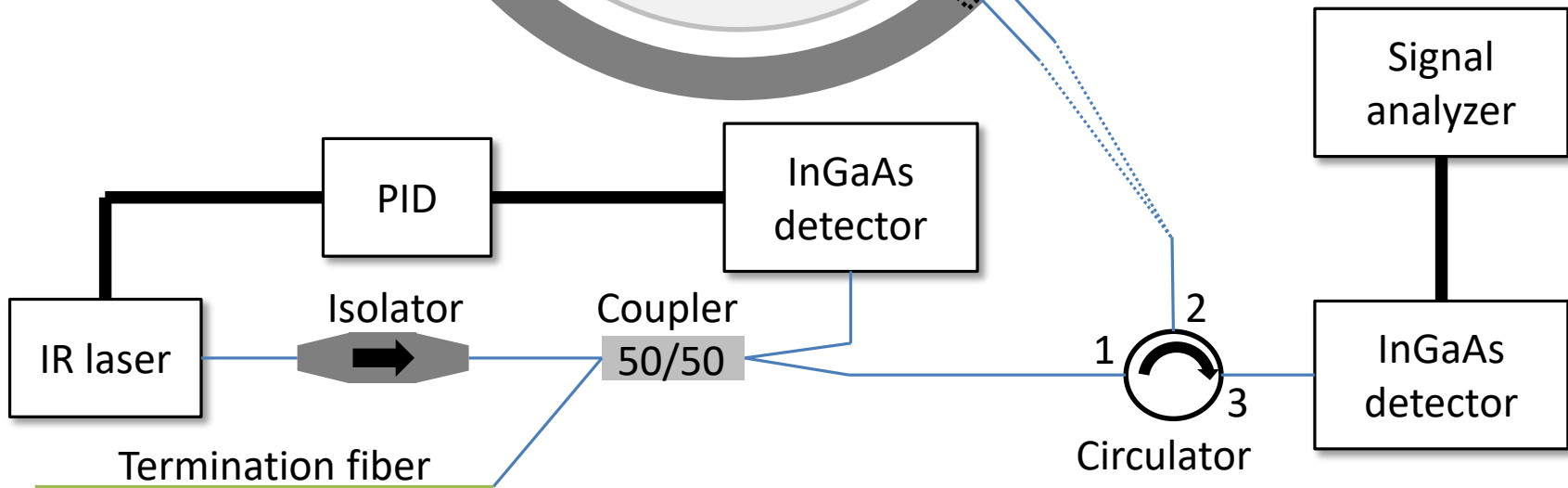
* Felipe Guzmán Cervantes, et al. *High sensitivity optomechanical reference accelerometer over 10 kHz*, Applied Physics Letters 104 (22), 221111 (2014).
 Felipe Guzmán Cervantes, et al. *Optomechanical motion sensors*, American Society of Precision Engineering, Conference on Precision Interferometry, 2015.

Felipe Guzmán Cervantes, et al. *MEMS optomechanical accelerometry standards*, American Society of Precision Engineering, Conference on Precision Interferometry, 2015.
 Yiliang Bao, Felipe Guzmán, et al. *An optomechanical accelerometer with a high-finesse hemispherical optical cavity*, IEEE Symposium on Inertial Sensors and Systems, 2016.

Experimental setup



- Low finesse cavity
- High finesse cavity
- Fiber optic
- Electrical connector

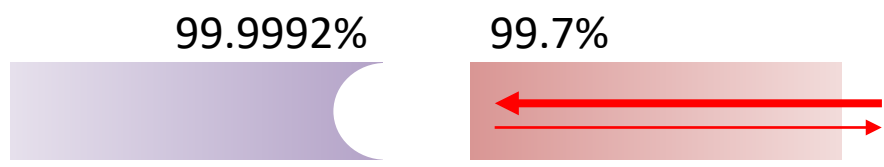


Displacement detection

$$\mathcal{F} \approx 1500$$

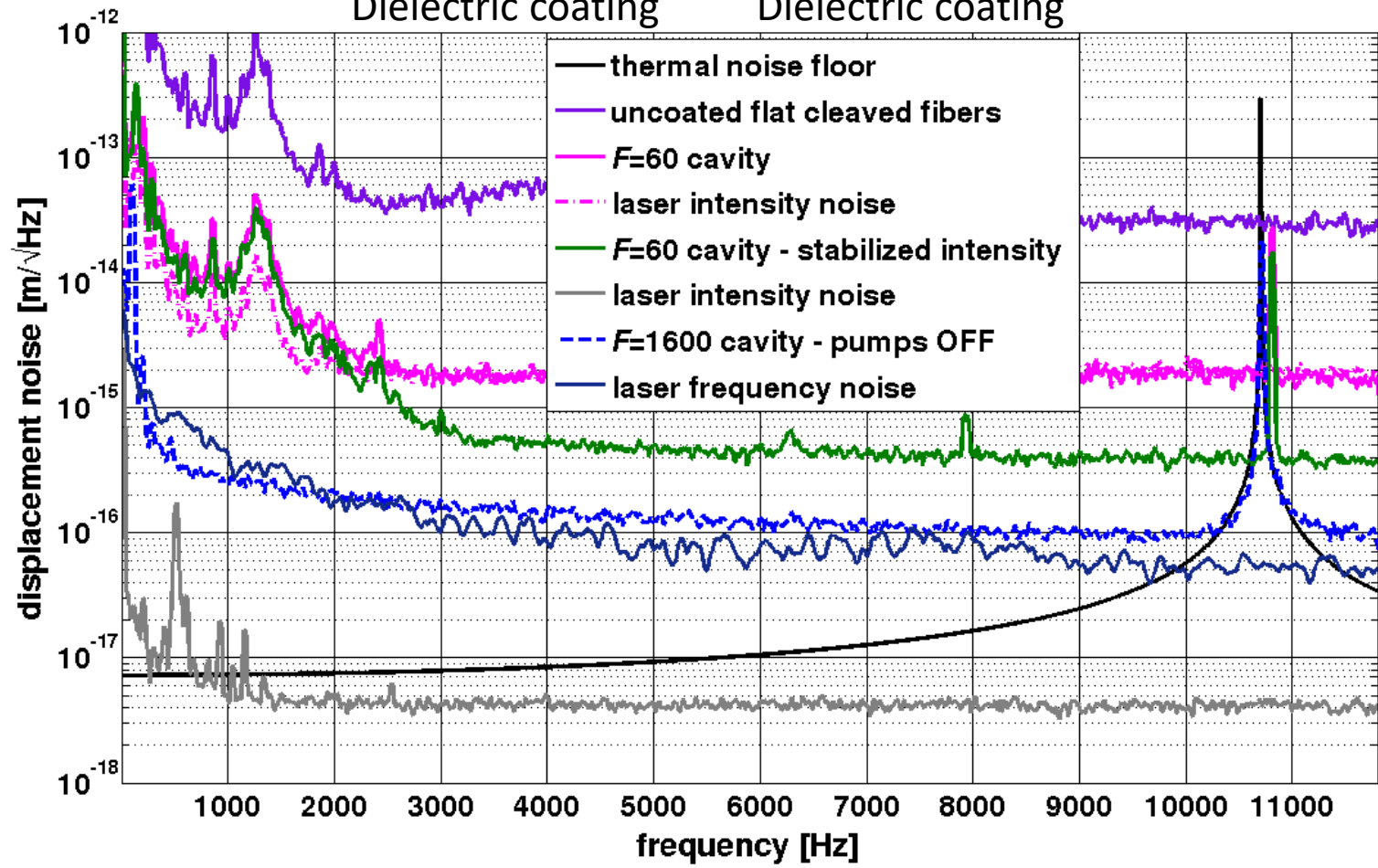
$$Q_{opt} \approx 430\,000$$

Low noise
laser



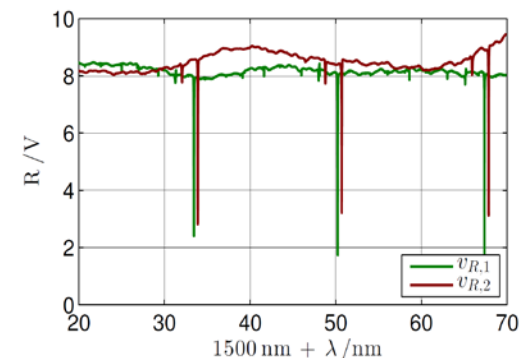
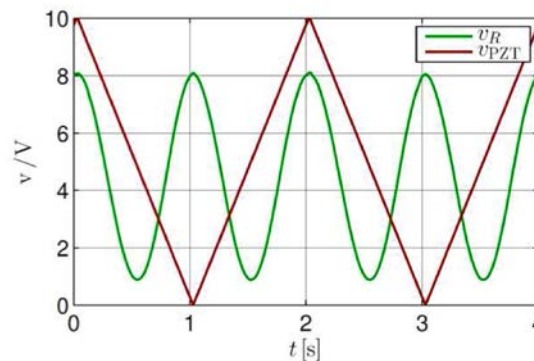
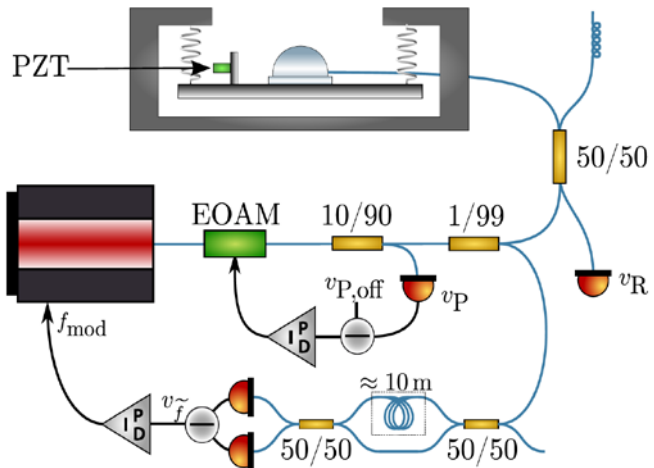
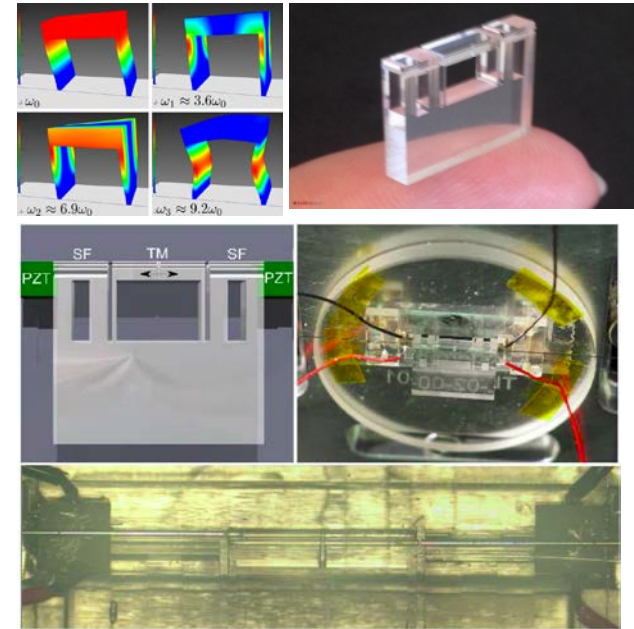
Laser ablated Dielectric coating Flat cleaved Dielectric coating

Visibility $\approx 97\%$



Optomechanical accelerometer - setup

- PZT tunes side-flexure cavities over a full fringe:
 - Cavities approximately $70\mu\text{m} \pm 0.5\ \mu\text{m}$
 - FSR: 2 THz, finesse: 1000, linewidth: 2 GHz
 - Range approx. $1.7\ \mu\text{m}$ (more than one fringe)
- Dual cavity readout – common-mode laser noise cancellation
 - Single cavity reaching $70\ \text{am}/\text{VHz}$ at high frequencies. $10\ \text{fm}/\text{VHz}$ @ 1 Hz.
- Laser, fiber-optic light distribution & modulators:
 - Laboratory grade equipment utilized so far.
 - Highly compact equivalent COTS components available.
 - Performance with COTS to be tested.
- Vibration isolation platform required for gravity and inertial sensing.



Optomechanical Gravimeters

- Ideal for space applications
 - Compatible materials and simple robust geometry
 - Cost-effective, small and light weight
 - Redundancy: dual test mass approach
 - Tunable performance space through smart and simple geometry
- Applications
 - Geodesy, Gravimetry, seismometry, structural analysis and control, quantum & fundamental physics, Inertial Navigation

• Performance limit

$$\underbrace{\delta a}_{SHO} = \sqrt{\frac{4k_B T \omega_0}{m_{eff} Q}}$$

• Lower resonance frequency

$$\delta a = \omega_0^2 \underbrace{\delta x}_{\substack{\text{displacement} \\ \text{noise density}}}$$

- Low stiffness flexures
 - Readout with large dynamic range ($> \lambda$)
 - Active test mass control / force rebalancing

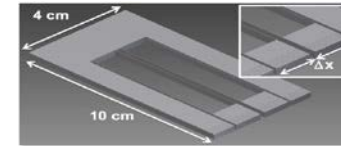
- Test mass: 10^{-3} kg, $Q: 2000$, $f_0=10$ Hz
- Dual test mass approach - redundancy
- Total sensor mass: < 30 g

• **Current acceleration sensitivity limit:**

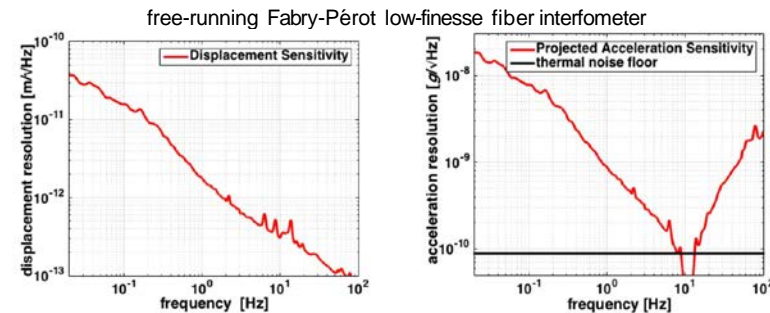
$$7 \times 10^{-10} \text{ m s}^{-2}/\sqrt{\text{Hz}}$$



$f_0 = 10$ Hz
 $m = 1000$ mg

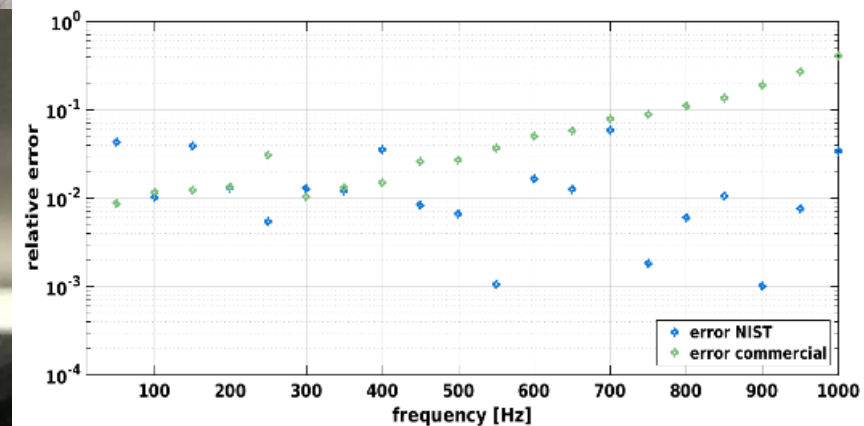
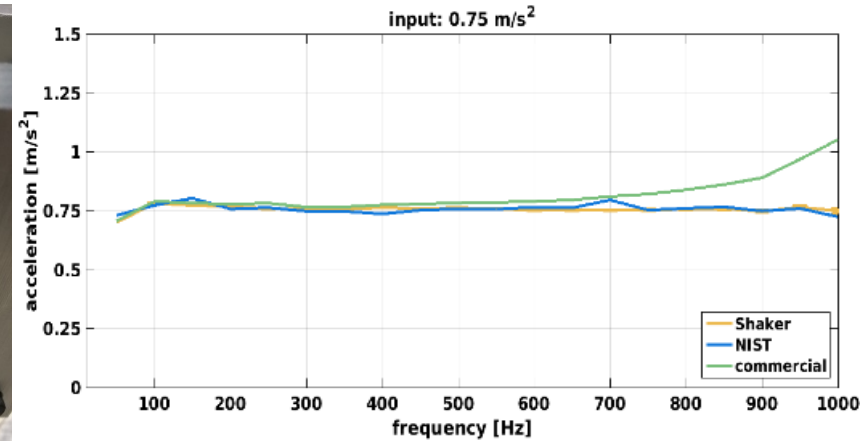
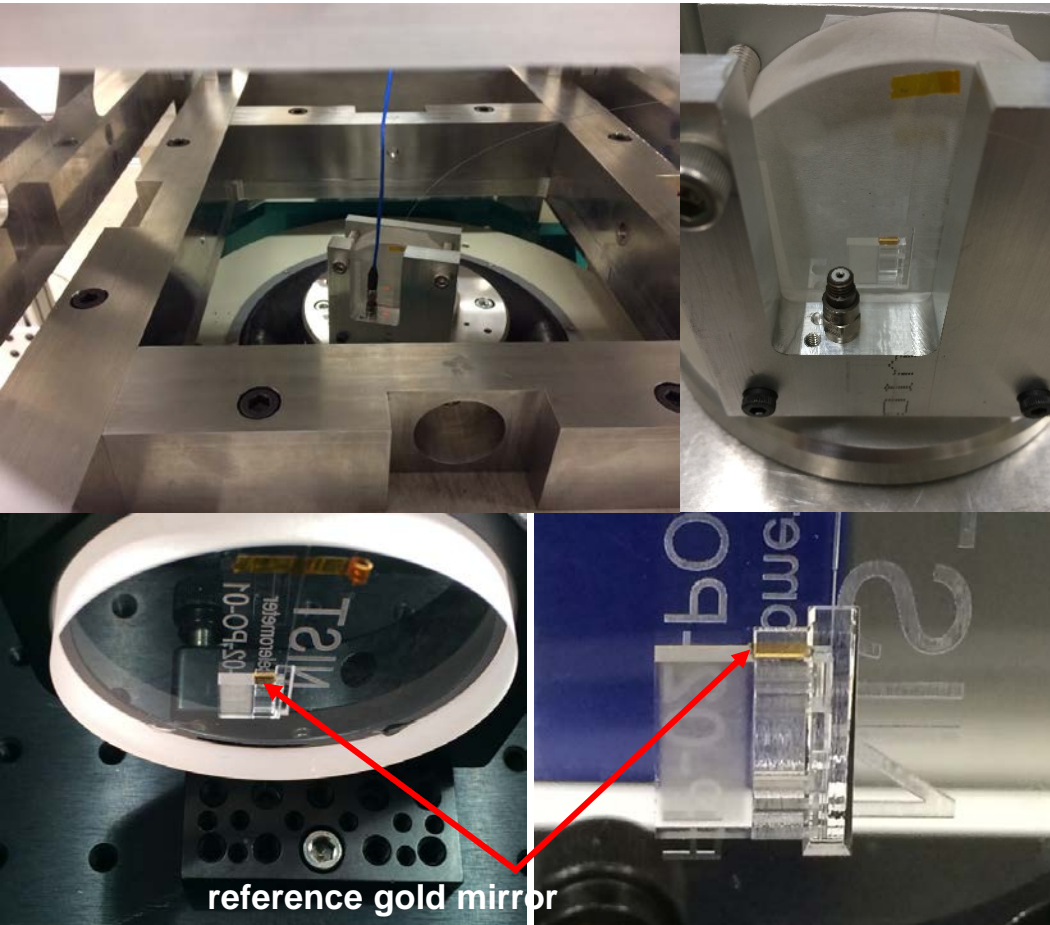


$$\frac{x(\omega)}{a(\omega)} = \frac{1}{\omega_0^2 - \omega^2 + \frac{i\omega_0}{Q} \omega}$$



Optomechanical accelerometer – primary standard

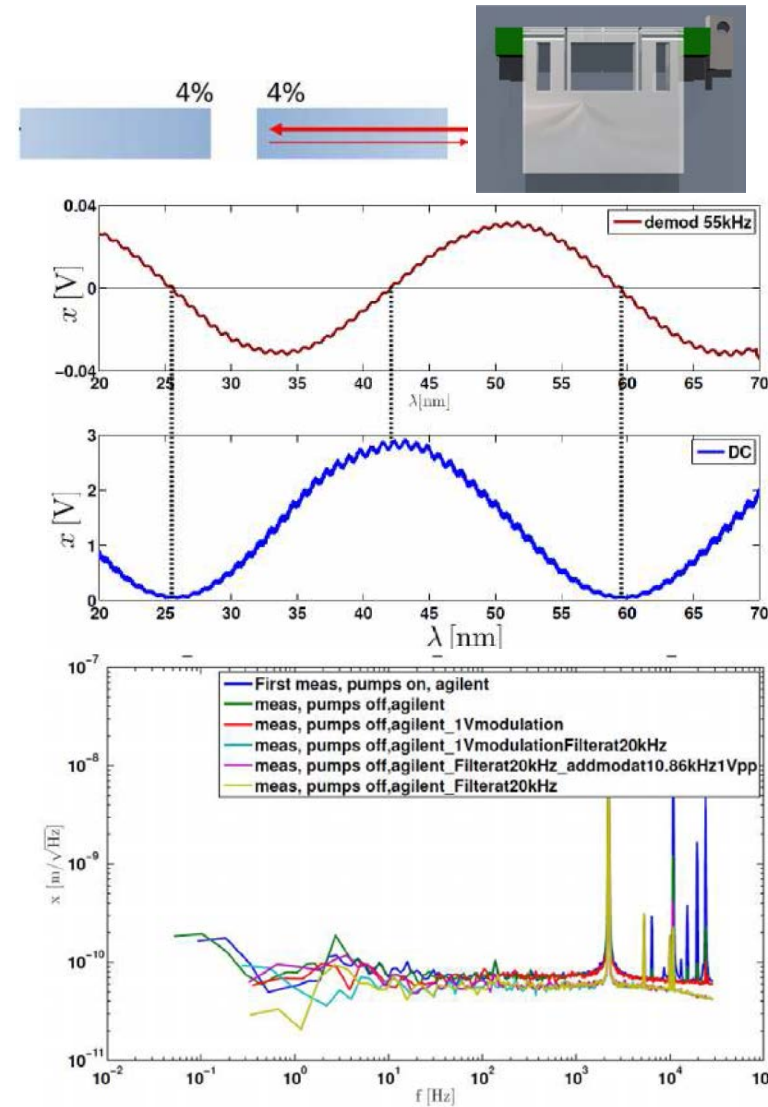
- National Metrology Institutes (NMI) state-of-the-art acceleration metrology
 - Comparison measurements against primary standards demonstrate NMI grade accuracies at levels of 10^{-3} – 10^{-2} .



Micro-optical motion sensors

- Low-finesse limit: bare glass 4% reflectivity
- Nearly sinusoidal response
- Extremely large *FSRs* \sim THz
- Enable absolute distance and displacement measurements
- DC read out sensitive to a few fm/vHz
- Mechanical modulation:
 - AC read out and servo technique
 - Provides error signal for cavity and laser control
 - Signal in quadrature from demodulation
 - Signals in quadrature for tracking over several fringes
- Preliminary tests show sensitivities of:

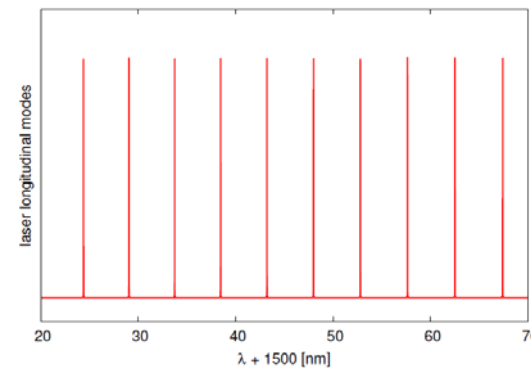
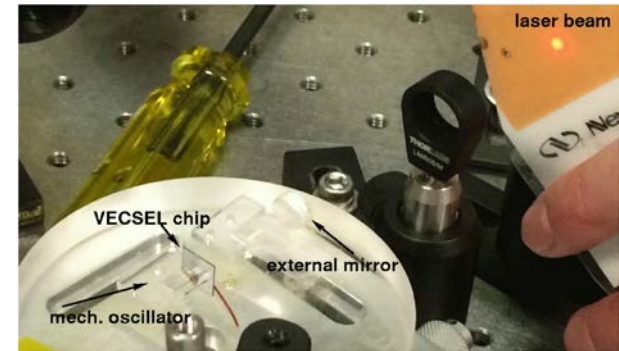
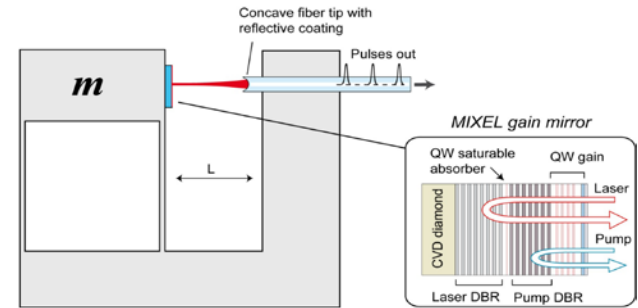
40-80 pm/vHz @ 10s mHz – 10s kHz



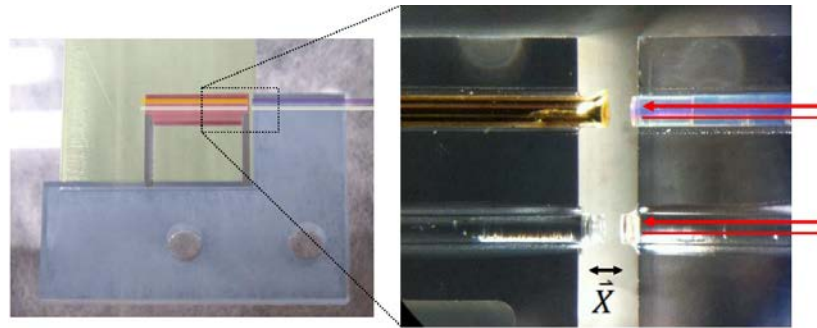
An Optomechanical Laser

Displacement to Frequency conversion

- VECSEL - Vertical-External-Cavity Surface-Emitting Laser:
 - Consists of surface-emitting chip (“half of a VCSEL”)
 - External mirror to complete laser cavity
 - Single-mode and Mode-locked operations possible
 - Optical pumping possible for high lasing power: > 10 W
 - Electrical pumping possible as well, lower optical output power
- Dynamics to Frequency transduction:
 - Dynamics: displacement, acceleration, force, inertial field and gravitational potential.
 - Test mass displacement → lasing cavity length changes
 - Test mass motion changes lasing frequency/wavelength
 - Mode-locked FSR / mode-beating → absolute measurement of cavity length
 - Absolute displacement measurements by using true frequency standards and their accuracies
- Frequency combs → THz down conversion:
 - Short cavities yield a coherent photonic THz source
 - Reference laser frequency combs
 - Compact and portable fiber combs



Thank you



Knowledge for Tomorrow

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- Yiliang Bao, Felipe Guzmán Cervantes, Arvind Balijepalli, John R Lawall, Jacob M Taylor, Thomas W. LeBrun, Jason J Gorman. An optomechanical accelerometer with a high-finesse hemispherical optical cavity. *IEEE International Symposium on Inertial Sensors and Systems*, 2016.
- Felipe Guzmán Cervantes, Oliver Gerberding, John Melcher, Julian Stirling, Jon R. Pratt, Gordon A. Shaw, and Jacob M. Taylor. Optomechanical motion sensors. *American Society of Precision Engineering, Conference on Precision Interferometry*, 2015.
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- F. Guzmán. American Geophysical Union (AGU) Meeting, Poster Contribution, San Francisco, CA, USA, December 2015.
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• Patent Applications

- Optomechanical Gravimeter** – Patent PS-2016-095, University of Maryland, US 62/355,208.
- Optomechanical Gravity Gradiometer** – Patent PS-2016-096, University of Maryland, , US 62/355,210.
- Optomechanical Laser** – Patent PS-2016-097, University of Maryland, , US 62/355,215.

